

# X-ray Sources

## Driven by high-intensity lasers

Jaroslav Nejdl

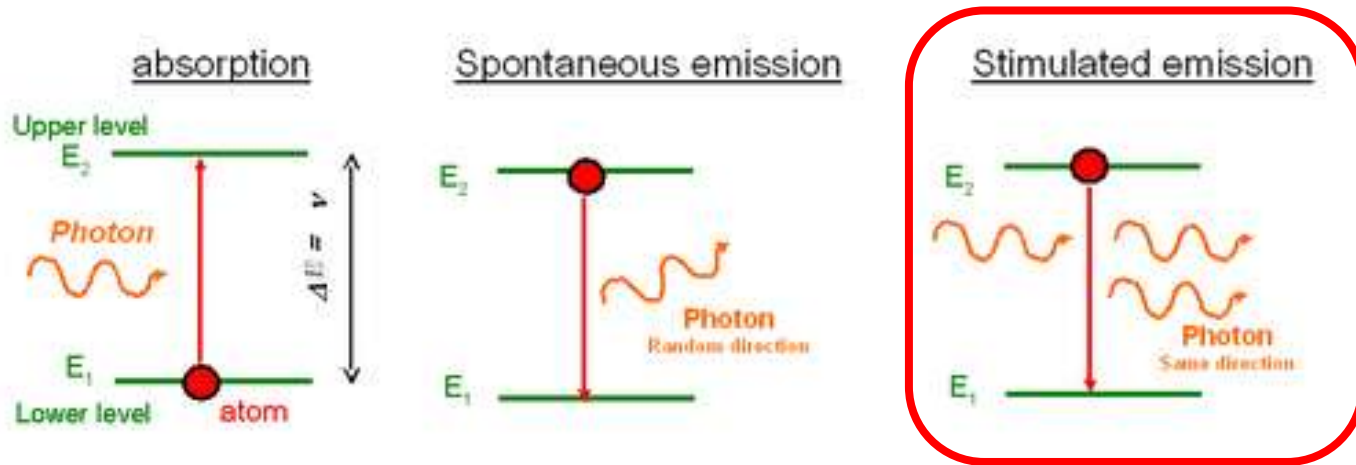
[nejdl@fzu.cz](mailto:nejdl@fzu.cz)

- Lasers with high peak power
- Origin of EM radiation: accelerated motion of charge
- High order Harmonic Generation
- Plasma-based X-ray lasers
- Laser-driven relativistic electron beams
  - Plasma betatron
  - Compton back-scattering
- X-ray plasma source ( $K\alpha$ )
- X-ray sources within ELI Beamlines research facility

# Lasers with high peak power

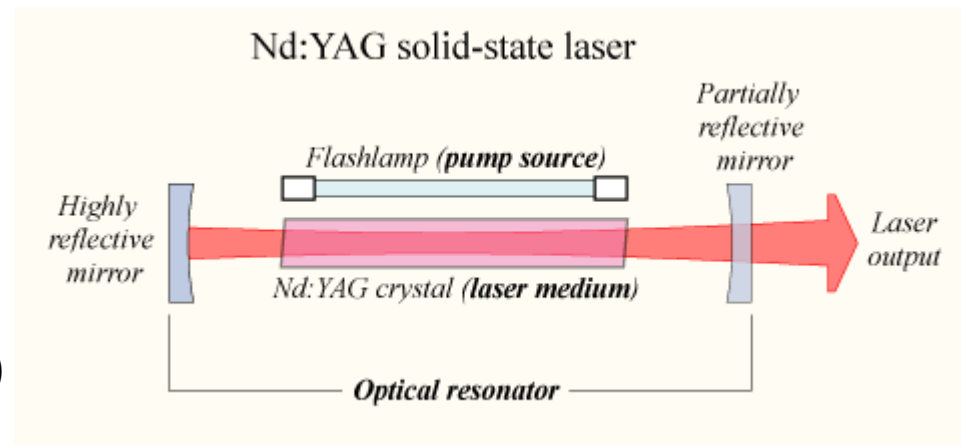
- Basic principles of laser

(**L**ight **A**mplified by **S**timulated **E**mission of **R**adiation)

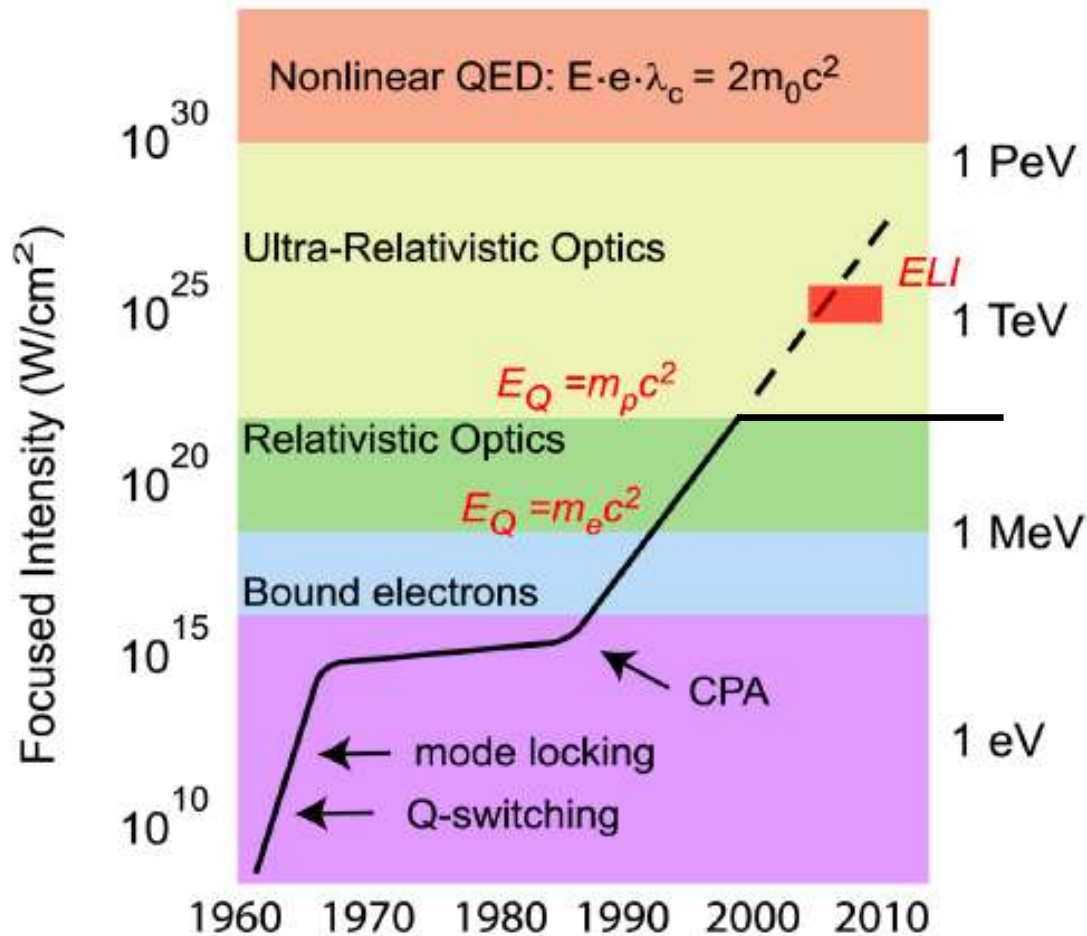


- Elements of lasers

- Gain medium
- Pumping
- Optical resonator (cavity)



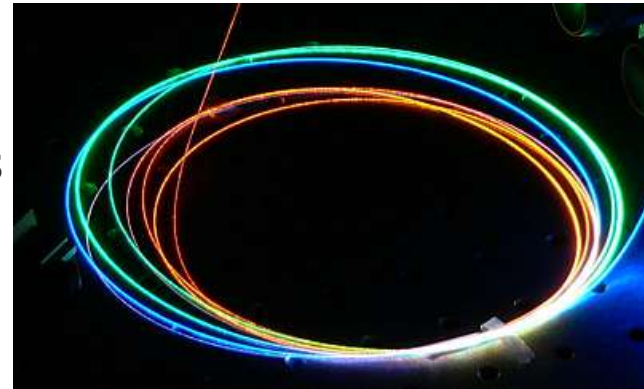
# Lasers with high peak power



# Lasers with high peak power

**Optical Kerr effect:**  $n(\mathbf{r}, t) = n_0 + n_2 I(\mathbf{r}, t)$

- solid (glas, crystals):  $n_2 \approx 10^{-16} \div 10^{-10} \text{ cm}^2 / \text{W}$
- air:  $n_2 \approx 4 \times 10^{-19} \text{ cm}^2 / \text{W}$
- $I = I(t)$  self-phase modulation
  - Generation of new frequencies (supercontinuum)

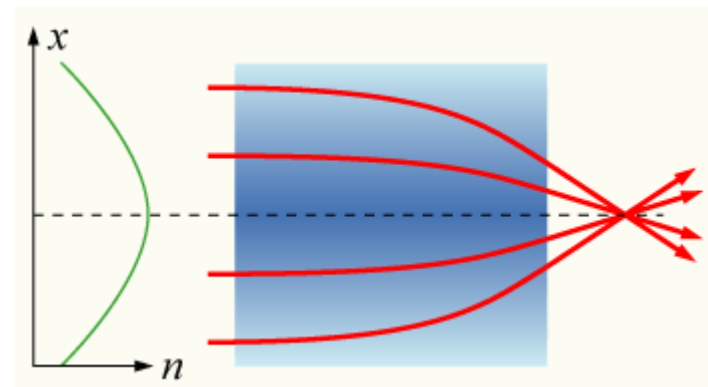


•  $I = I(\mathbf{r})$  self-focusing

• Critical power  $P_{cr} \approx 0.15 \frac{\lambda^2}{n_0 n_2}$

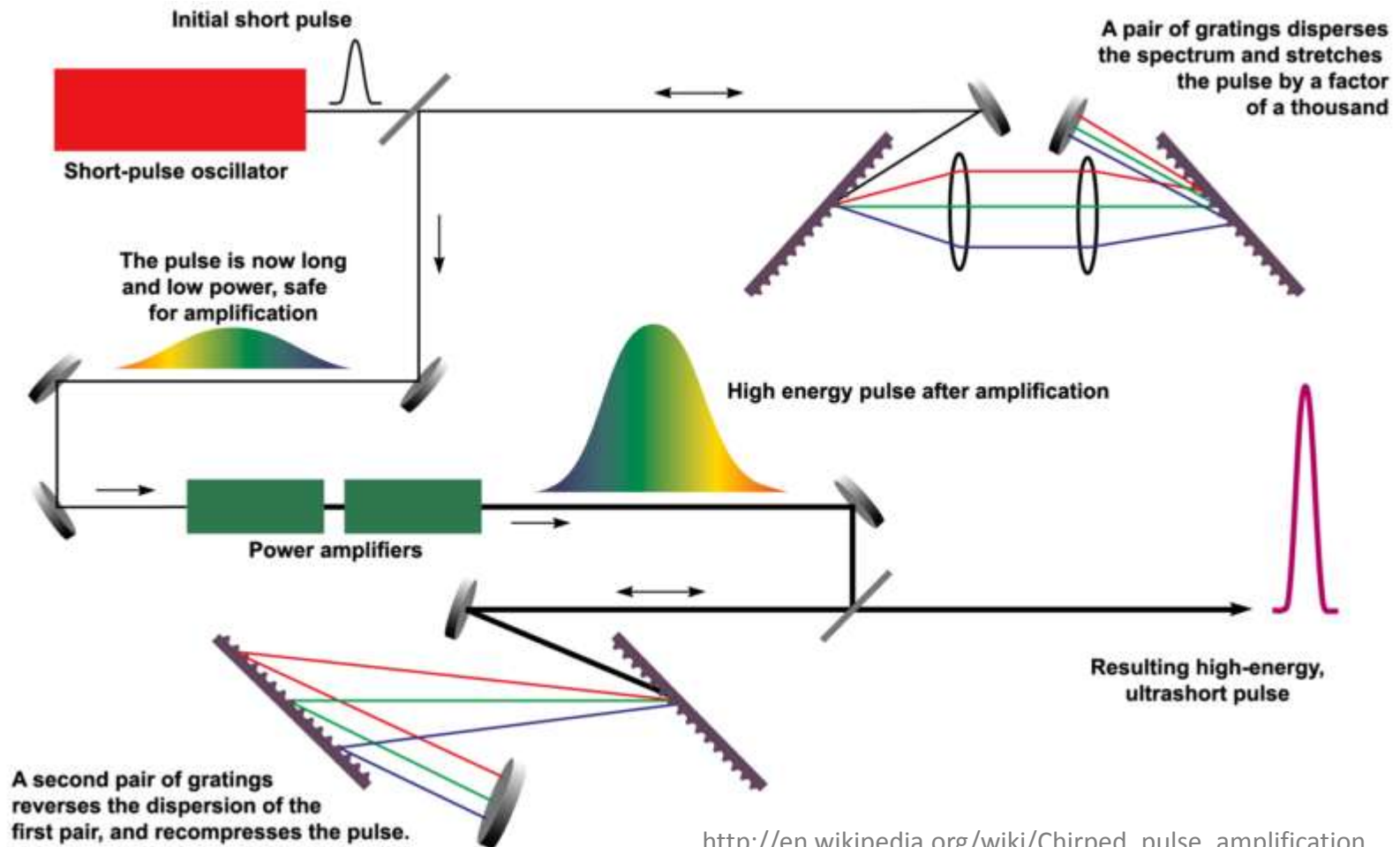
• 800nm : glass:  $P_{cr} \approx 2\text{MW}$

air:  $P_{cr} \approx 2\text{GW}$



# Lasers with high peak power

- Increasing the peak power → self-focusing → DAMAGE
- Solution : Chirped pulse amplification (CPA)



# Lasers with high peak power

- Intensity (Irradiance)

Energy delivered per unit time to unit area

$$I \approx \frac{E}{\tau S} = \frac{P}{S} \text{ [Wm}^{-2}\text{]}$$

- Area depends on the focusing

- Focus diameter given by  $d \propto \frac{f\lambda}{\Phi}$

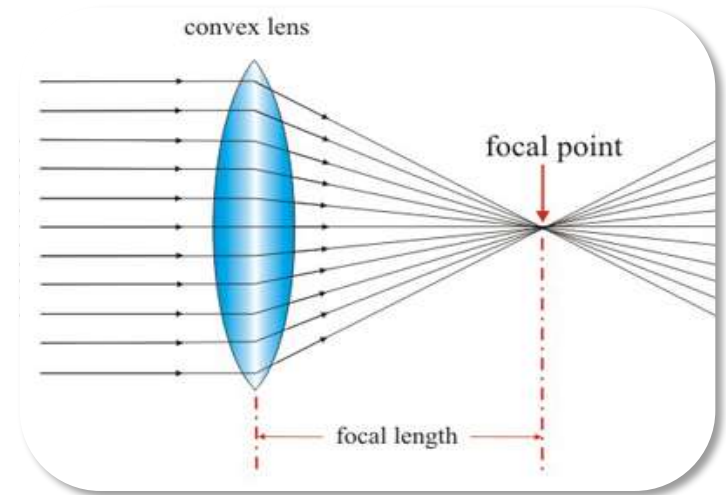
- Laser wavelength  $\lambda$ , focal length  $f$ , beam size  $\Phi$ , wavefront quantity
- Mostly given by the laser parameters ( $\lambda \approx 1\mu\text{m}$ ,  $\Phi < 50\text{cm}$ )

- World records:

- Energy in a pulse  $E = 4 \text{ MJ} = 4 \times 10^6 \text{ J}$  (NIF, LMJ)
- Pulse duration  $\tau = 3 \text{ fs} = 3 \times 10^{-15} \text{ s}$

These extremes weren't achieved simultaneously,  $P_{\text{max}} \approx 1 \text{ PW} = 10^{15} \text{ W}$

- Intensity  $I = 10^{22} \text{ Wcm}^{-2}$



# Lasers with high peak power

Highest energy in a (long) pulse



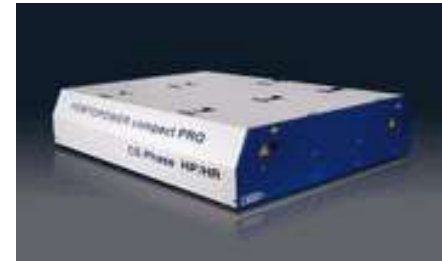
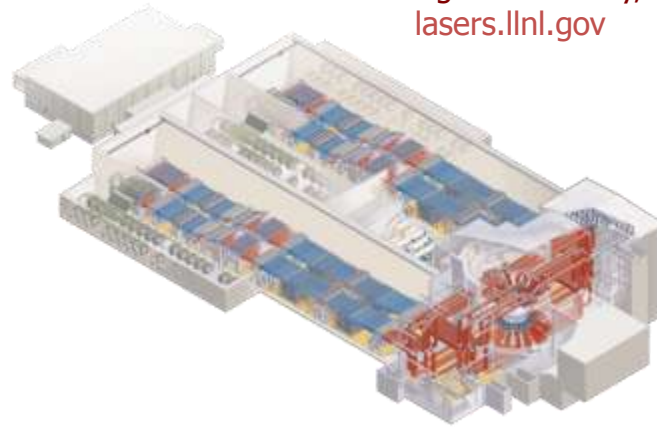
Shortest pulses



Highest peak power



NIF: National Ignition Facility, USA 2009  
[lasers.llnl.gov](http://lasers.llnl.gov)



ELI: Extreme Light Infrastructure (2015)  
[eli-beams.eu](http://eli-beams.eu)

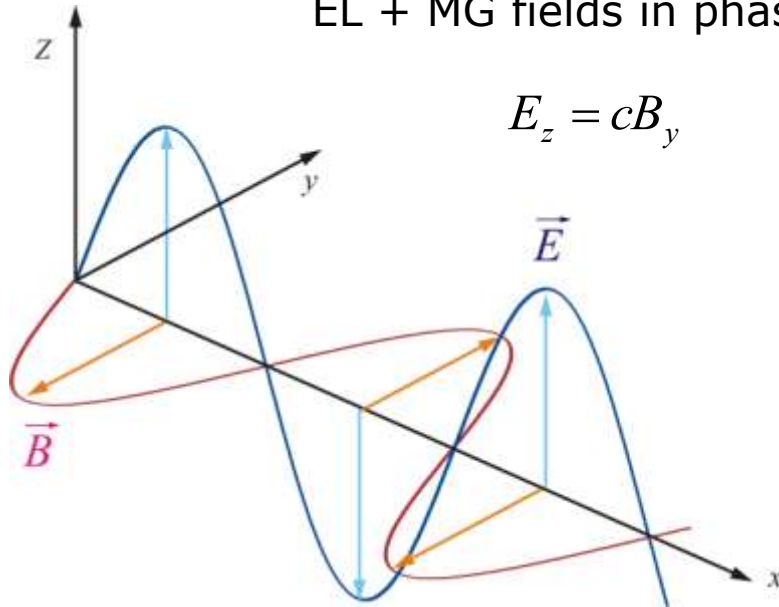




# Lasers with high peak power

## Electron / proton motion in the intense laser field

EL + MG fields in phase



$$\frac{d\mathbf{p}}{dt} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

If  $v \ll c$  ( $I < 10^{18} \text{ Wcm}^{-2}$ )

Effect of the magnetic field negligible

If  $v \approx c$  contribution of  $E$  and  $B$  comparable

⇒ Force pushing the particles

in the direction of laser propagation

If  $I = 10^{18} \text{ Wcm}^{-2}$  the amplitude of the field  $E = 2.75 \times 10^{12} \text{ Vm}^{-1}$

electron: for  $\lambda = 800 \text{ nm}$   $v = 0.974c$  in  $\frac{1}{2}$  cycle of the laser field

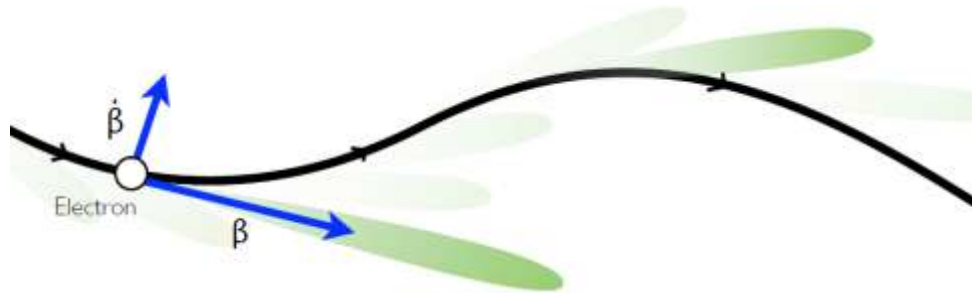
If  $I = 10^{24} \text{ Wcm}^{-2}$  the field amplitude  $E = 2.75 \times 10^{15} \text{ Vm}^{-1}$

proton: for  $\lambda = 800 \text{ nm}$   $v = 0.92c$  in  $\frac{1}{2}$  cycle of the laser field

# Origin of EM radiation

Microscopically: accelerated motion of a charge

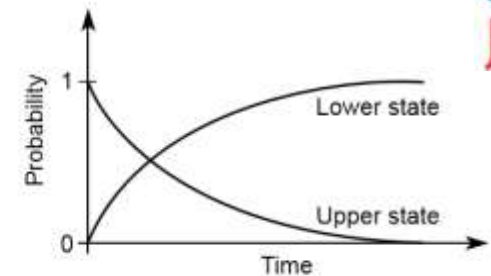
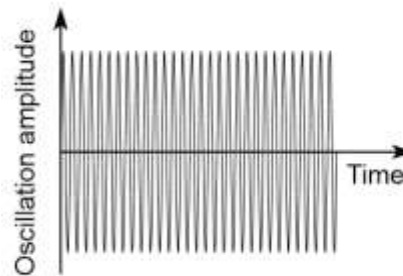
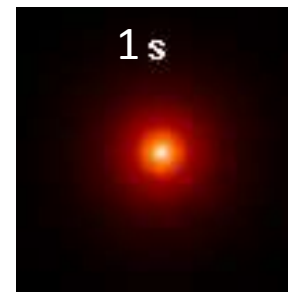
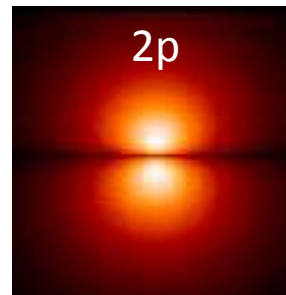
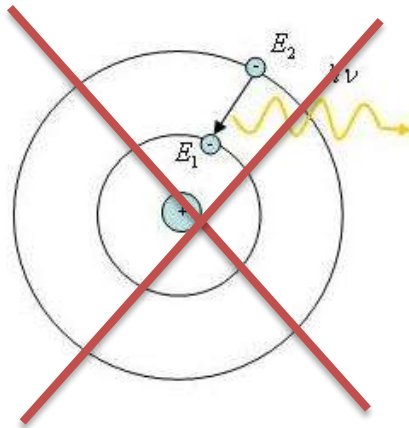
- Free:



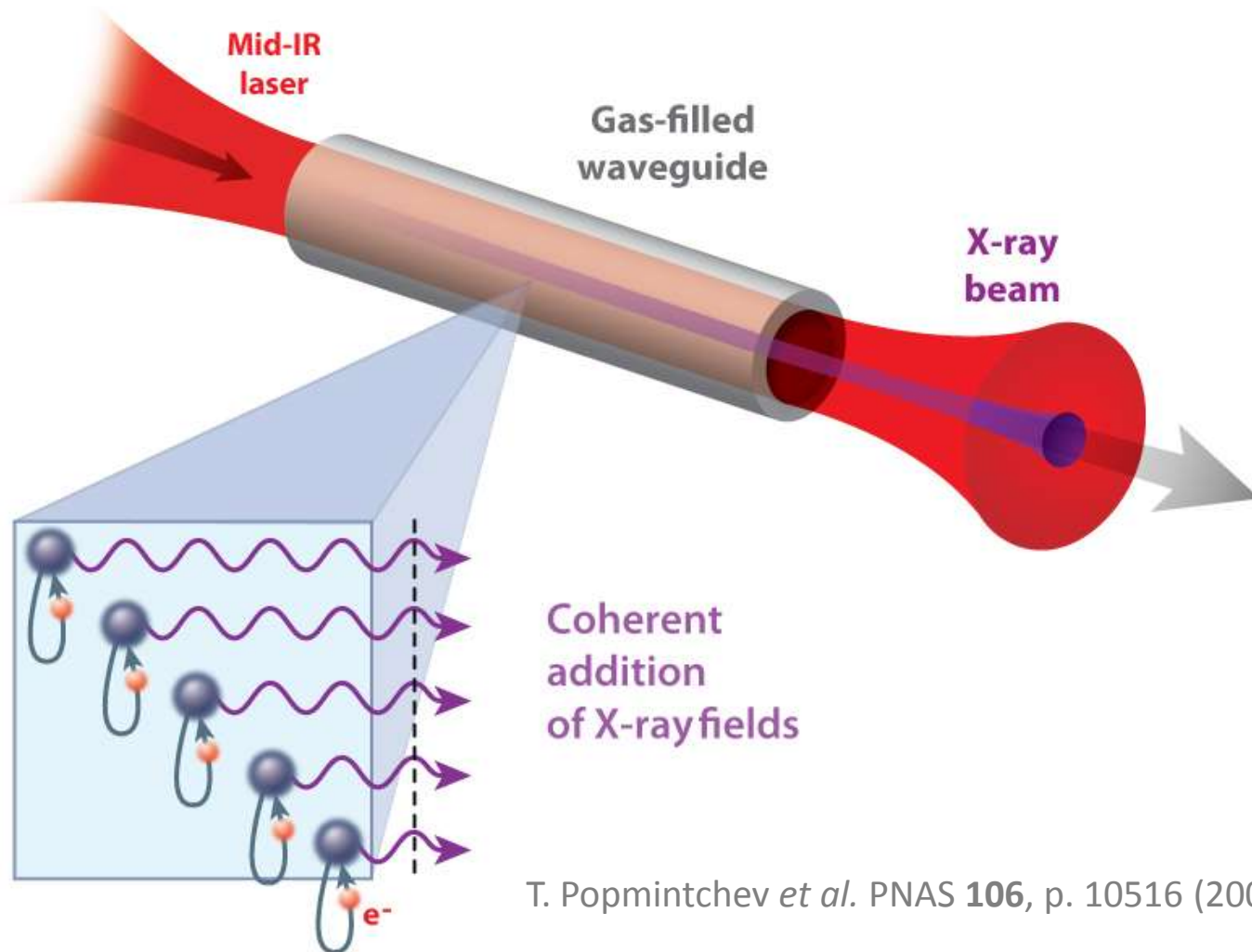
$$\frac{d^2I}{d\omega d\Omega} = \frac{e^2}{4\pi^2 c} \left| \int_{-\infty}^{+\infty} e^{i\omega[t-\vec{n}\cdot\vec{r}(t)/c]} \frac{\vec{n} \times [(\vec{n} - \vec{\beta}) \times \dot{\vec{\beta}}]}{(1 - \vec{\beta} \cdot \vec{n})^2} dt \right|^2$$



- Bound: radiative (allowed) transitions



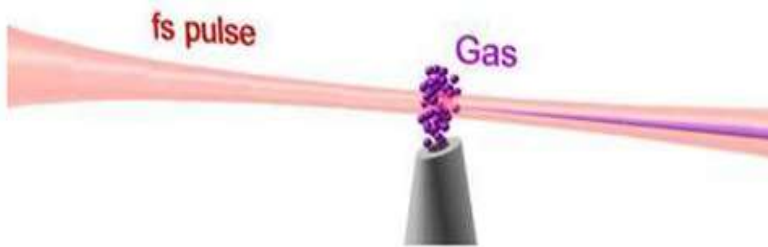
# High-order harmonic generation



T. Popmintchev *et al.* PNAS **106**, p. 10516 (2008)

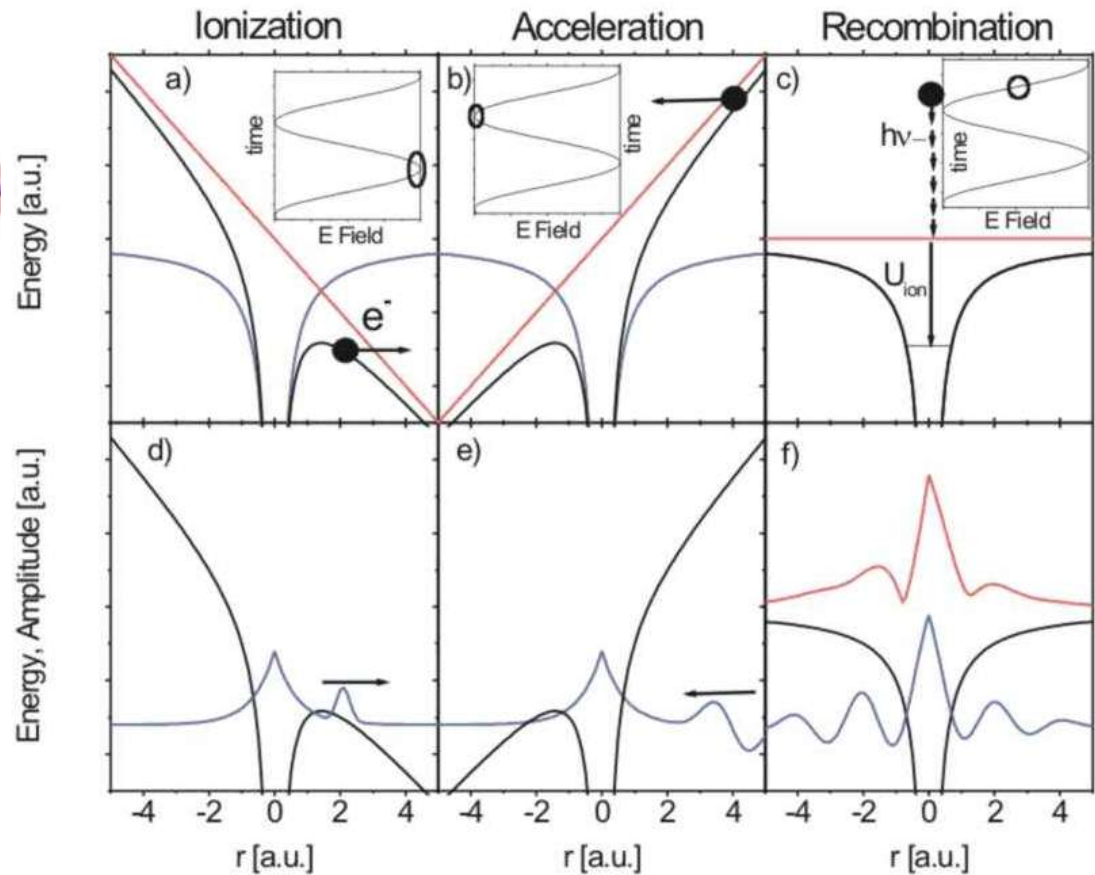
# High-order harmonic generation

- Interaction of linearly polarized intense laser pulse with matter (valence electron)



- Three step model:
  - Ionization
  - Acceleration
  - Recombination

P. B. Corkum, Phys. Rev. Lett., **71**, 1994 (1993)



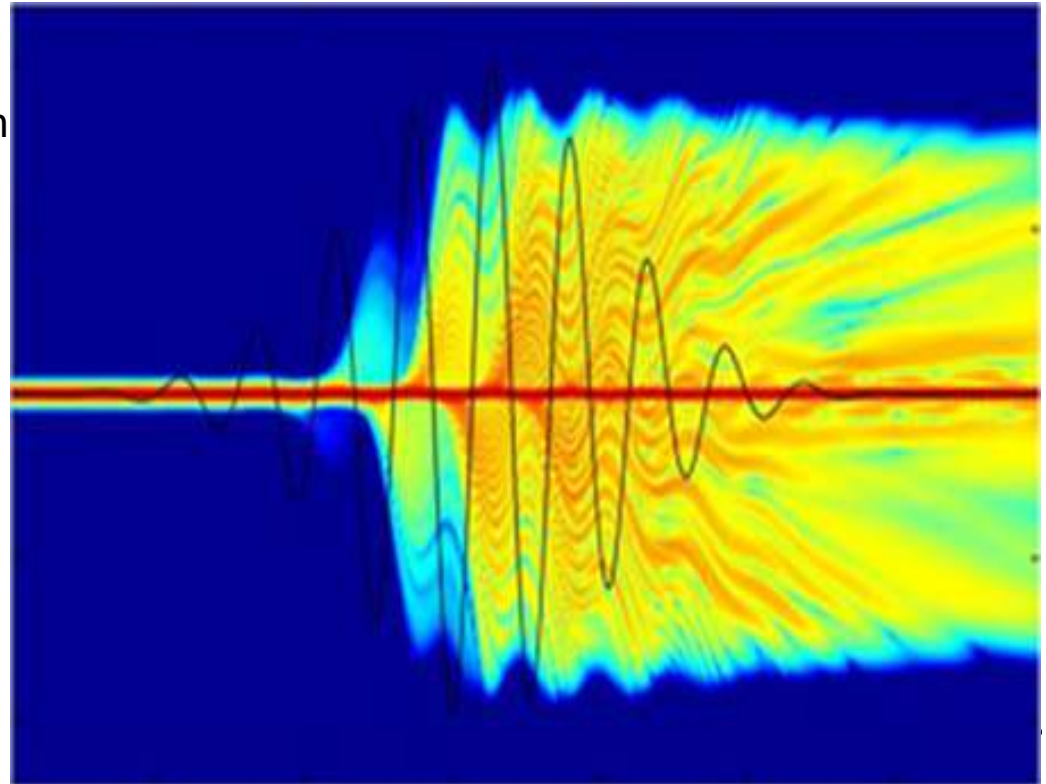
# High-order harmonic generation

- Quasi-monochromatic radiation + centro-symmetrical medium → **odd harmonics only**

- Microscopic analysis  
Dipole momentum of a single atom

$$E_{cutoff} \approx I_p + 3.17 U_p$$

- Macroscopic analysis  
absorbtion, phase-matching,  
diffraction



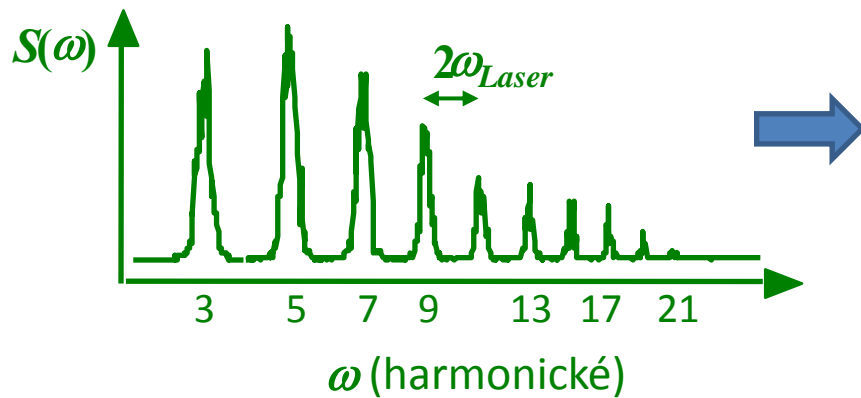
Electron density  $|\psi(x,t)|^2$

# High-order harmonic generation

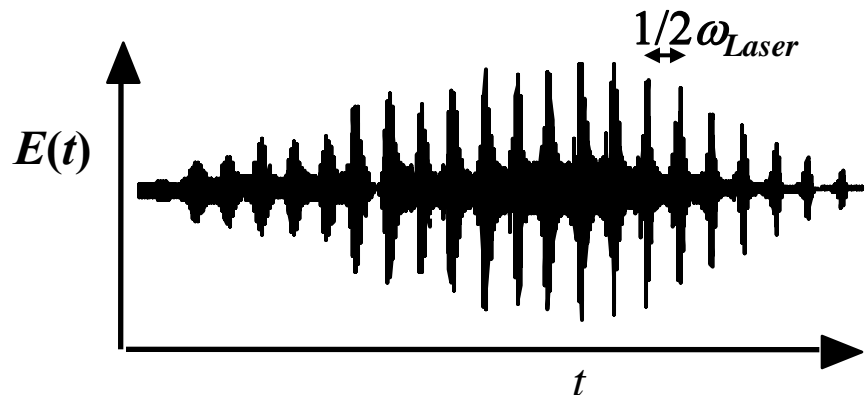
- $\lambda = 800 \text{ nm} \rightarrow T = 2.7 \text{ fs}$   
 $\rightarrow h\nu = 1.55 \text{ eV}$

100fs laser pulse: attosecond pulse train

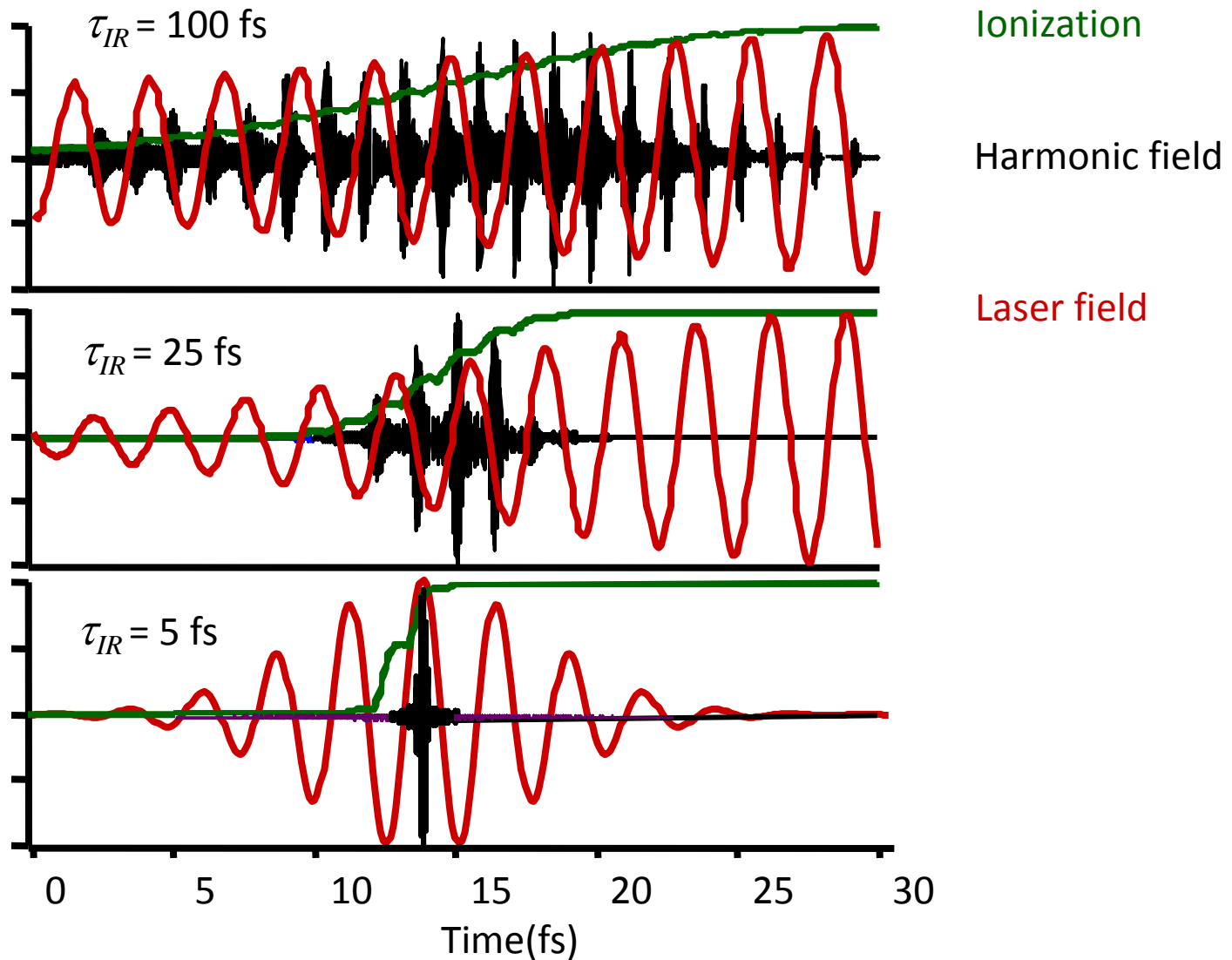
Measured spectrum



Estimated E-field evolution



# High-order harmonic generation



## Tailoring a 67 attosecond pulse through advantageous phase-mismatch

Kun Zhao,<sup>1</sup> Qi Zhang,<sup>1</sup> Michael Chini,<sup>1</sup> Yi Wu,<sup>1</sup> Xiaowei Wang,<sup>1,2</sup> and Zenghu Chang<sup>1,\*</sup>

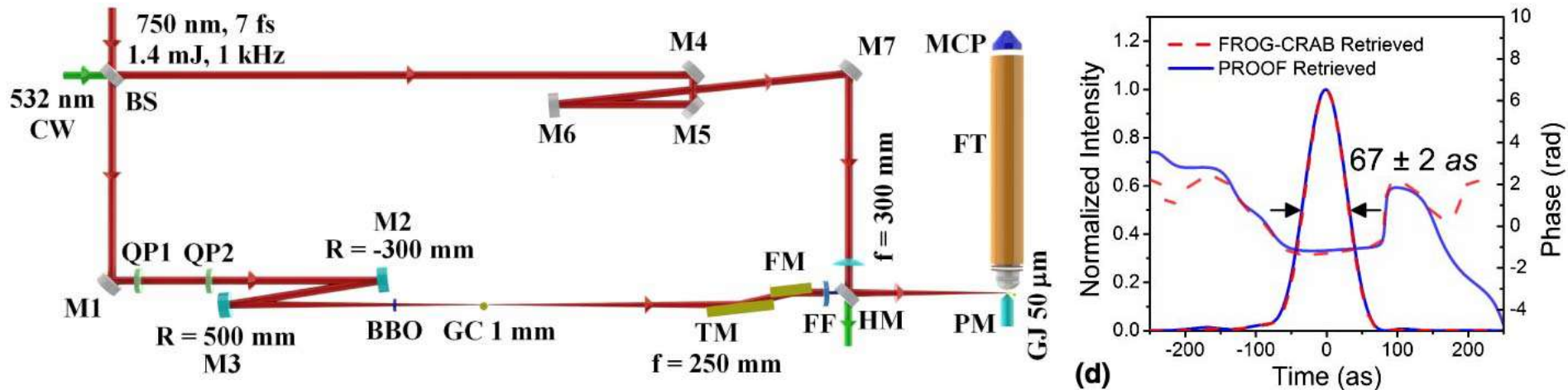
<sup>1</sup>Department of Physics and CREOL, University of Central Florida, Orlando, Florida 32816, USA

<sup>2</sup>Department of Physics, National University of Defense Technology, Changsha, Hunan, China

\*Corresponding author: Zenghu.Chang@ucf.edu

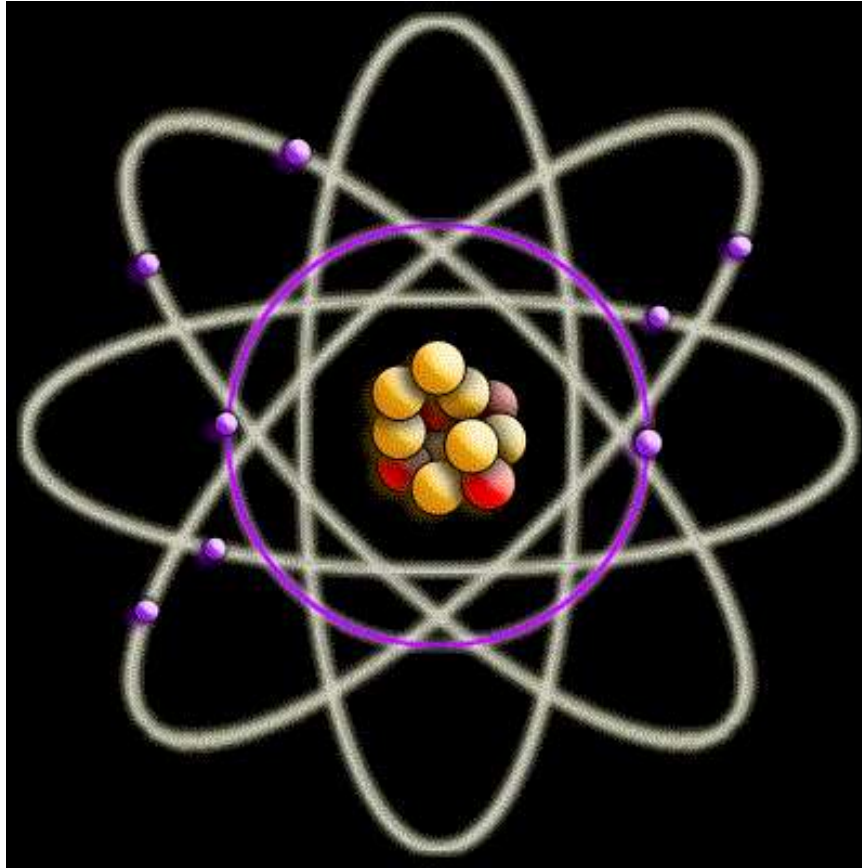
Received May 24, 2012; revised July 25, 2012; accepted August 13, 2012;  
 posted August 13, 2012 (Doc. ID 169268); published September 14, 2012

A single isolated attosecond pulse of 67 as was composed from an extreme UV supercontinuum covering 55–130 eV generated by the double optical gating technique. Phase mismatch was used to exclude the single-atom cutoff of the spectrum that possesses unfavorable attochirp, allowing the positive attochirp of the remaining spectrum to be compensated by the negative dispersion of a zirconium foil. Two algorithms, PROOF and FROG-CRAB, were employed to retrieve the pulse from the experimental spectrogram, yielding nearly identical results. © 2012 Optical Society of America



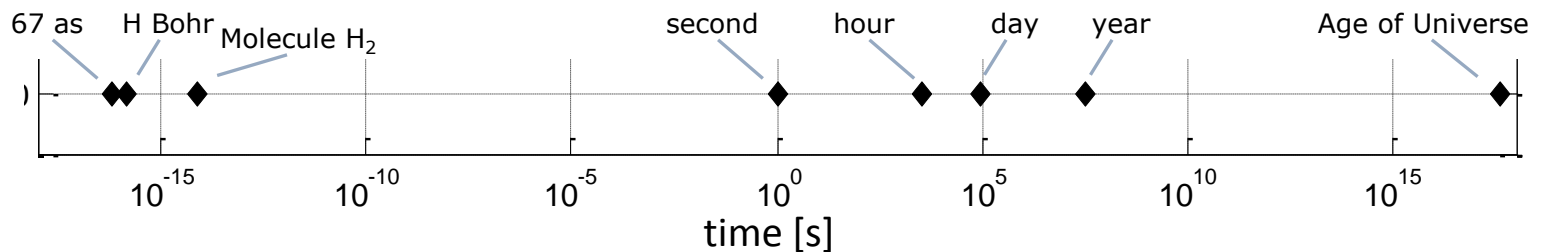


# High-order harmonic generation

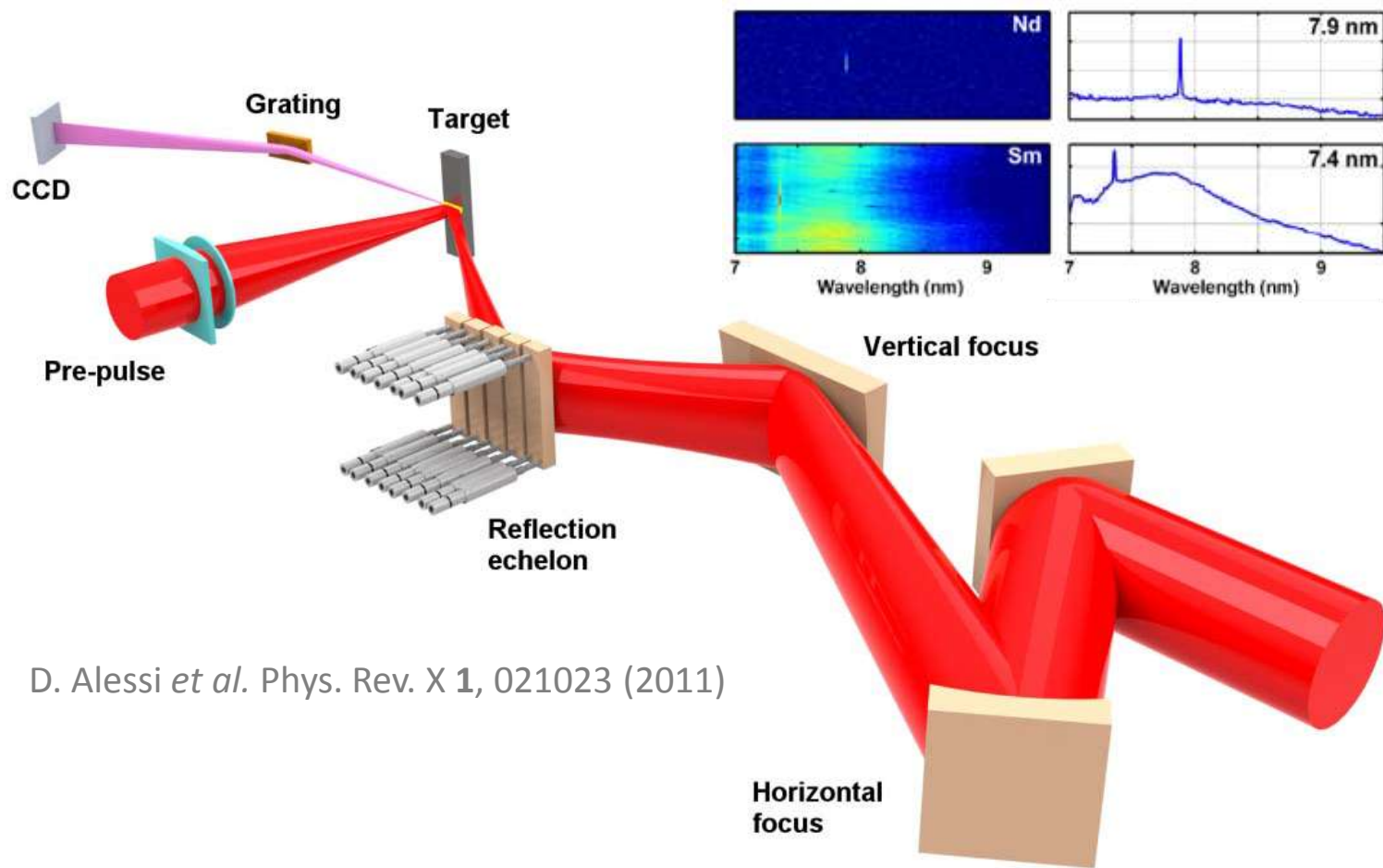


Period of an electron in Bohr's orbital of hydrogen:  
 $T = 152 \text{ as}$

Period of vibration of  $\text{H}_2$   
 $T = 8 \text{ fs}$



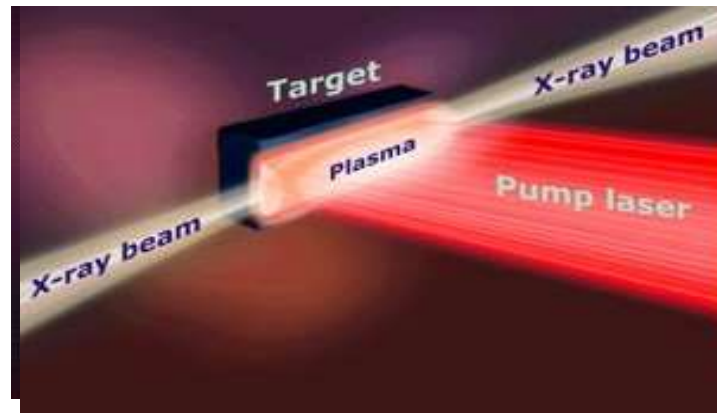
# Plasma-based x-ray lasers



D. Alessi *et al.* Phys. Rev. X **1**, 021023 (2011)

# Plasma-based x-ray lasers

- Employ radiative transitions of multiply ionized matter
  - Energy difference between levels increases with the charge
  - Gain medium is a narrow column of hot highly ionized plasma



Ex] hydrogen-like ion (H-like)

$Z$  – proton number

$n_i$  – principal quantum number

$\tau$  – lifetime of upper level

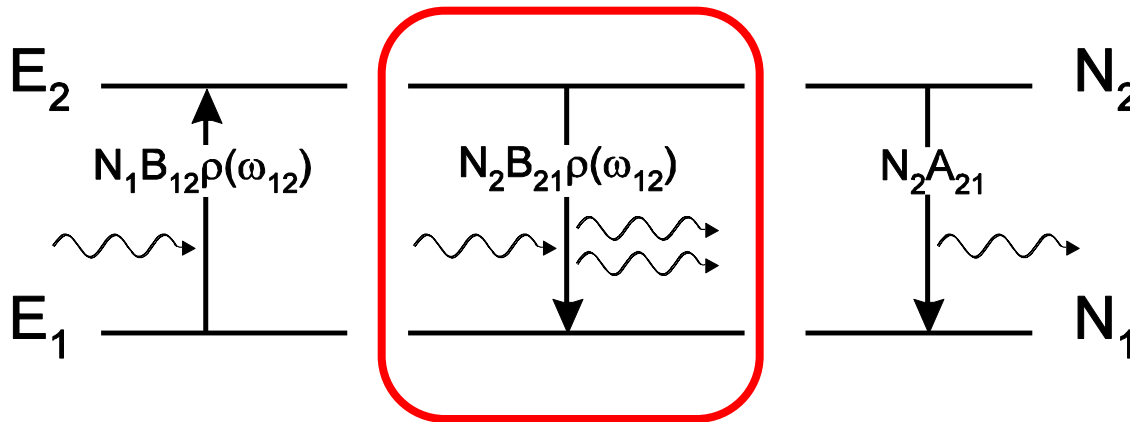
$$E_u - E_l = (13.6\text{eV}) Z^2 \left( \frac{1}{n_l^2} - \frac{1}{n_u^2} \right)$$

$$\hbar\omega \propto Z^2, \quad \tau \propto 1/Z^4$$

H-like C  $\equiv$  C<sup>+5</sup>  $\equiv$  C VI (spectroscopical notation):

transition 2p – 1s:  $\hbar\omega = 367\text{eV}$ ,  $\lambda = 3.4\text{ nm}$ ,  $\tau = 1.2\text{ ps}$

## Einstein's coefficients



From the detailed balance:

$$\frac{A_{21}}{B_{21}} = \frac{\hbar \omega_{21}^3}{\pi^2 c^3} \propto \lambda^{-3} \quad (1)$$

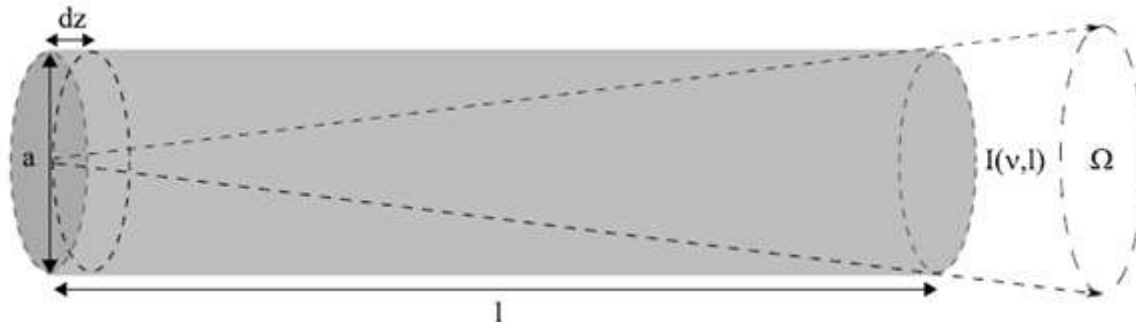
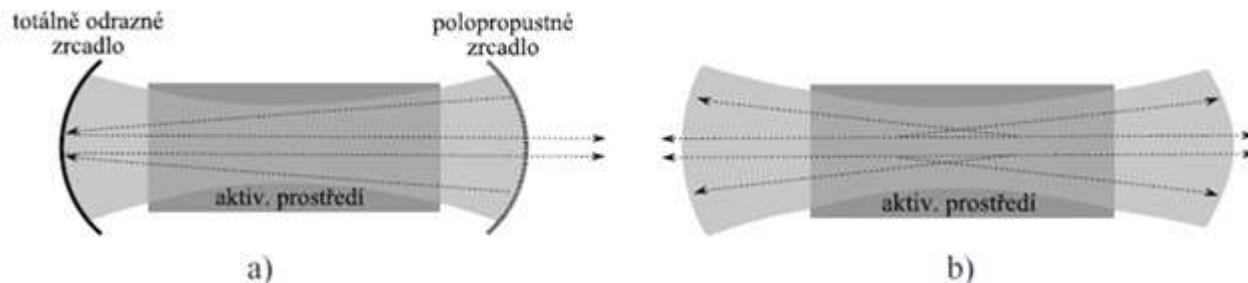
A,B depends only on the quantum system  $\Rightarrow$  relation (1) is valid even outside equilibrium

Pumping intensity is proportional to  $1/\lambda^4 \Rightarrow$  high pump power for shorter wavelengths – possible only in hot dense plasma

# Plasma-based x-ray lasers

Due to **short lifetimes** of the gain, nonexistence of **highly reflecting mirrors** in XUV/x-ray and **agressive plasma** (damages nearby optics)  
**Laser resonator (cavity) cannot be used**

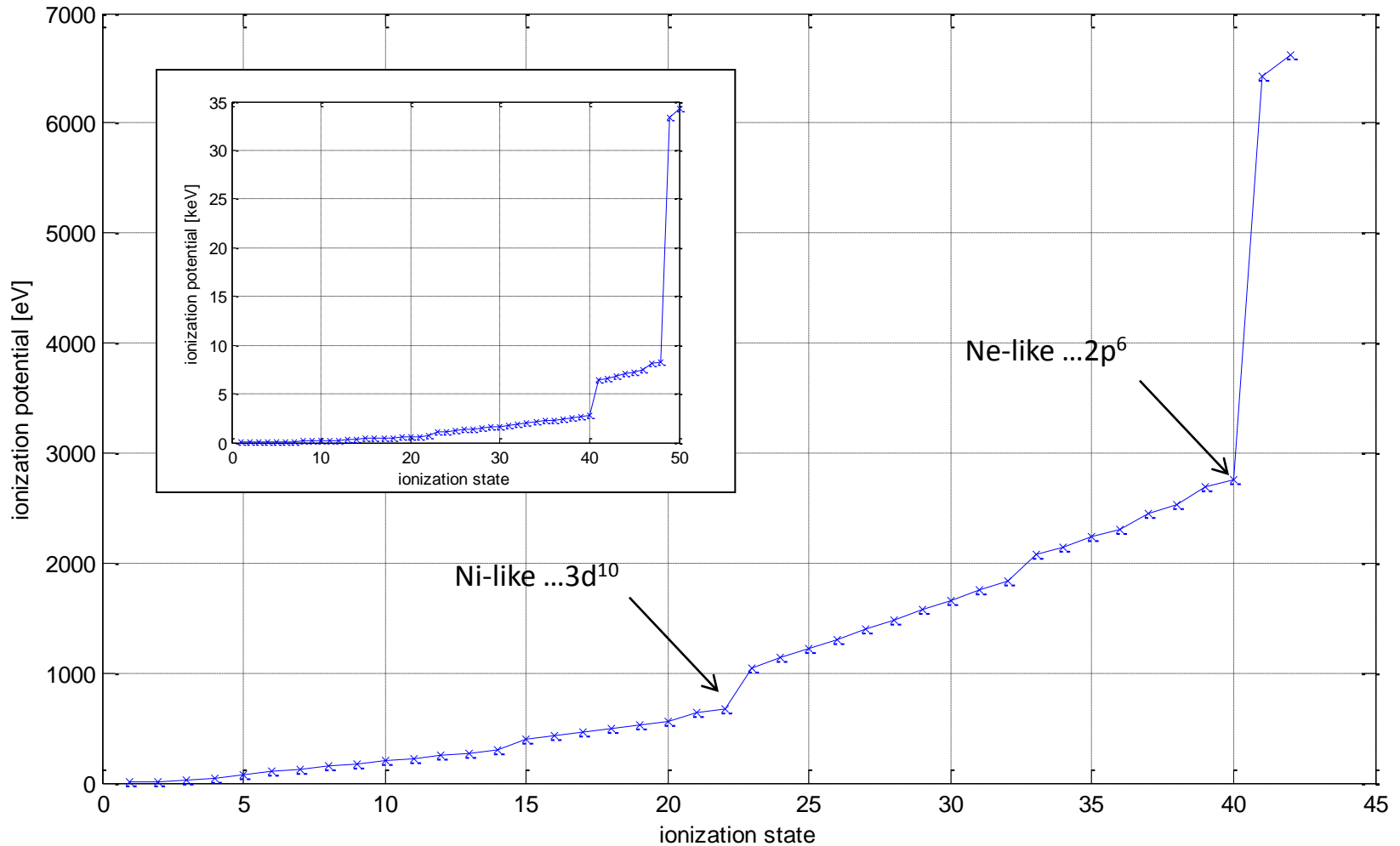
We rely on **Amplified Spontaneous Emission (ASE)**  
 (amplified noise– effects on wavefront, coherence...)



# Plasma-based x-ray lasers

Example: Sn: Z=50

Ground state  $1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^2 4p^6 4d^{10} 5s^2 5p^2$



# Plasma-based x-ray lasers

Solving Saha equation for (Sn) plasma:  $Z=50$

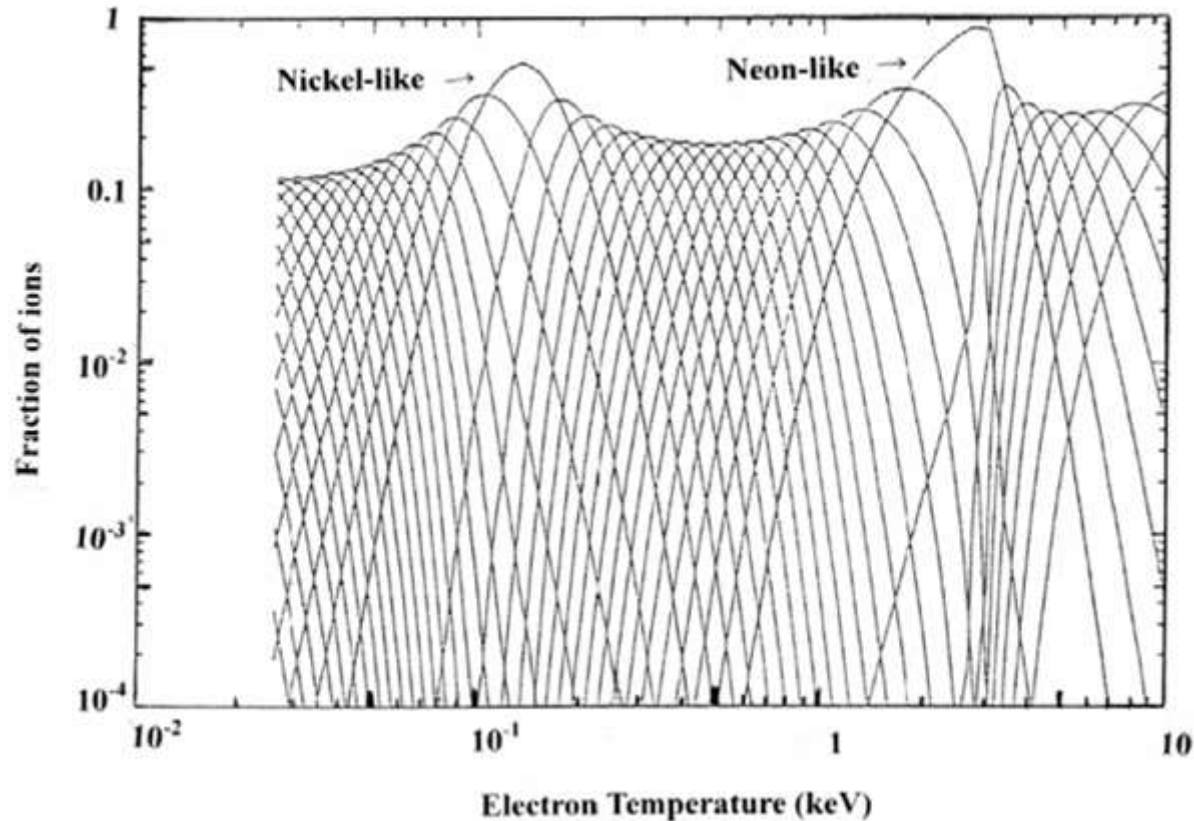


Figure 11. Ion abundance as a function of the electron temperature for tin plasma.

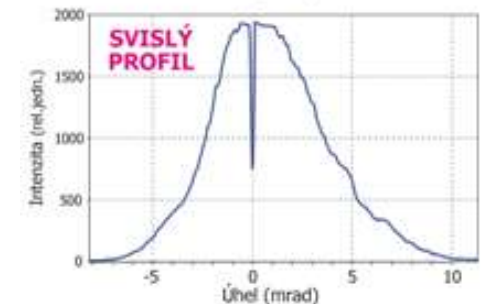
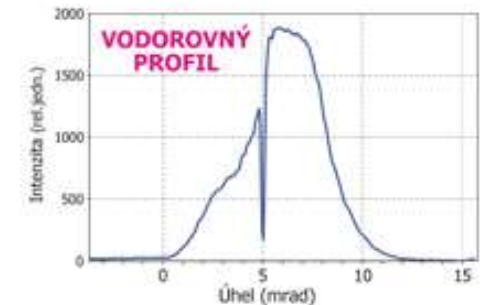
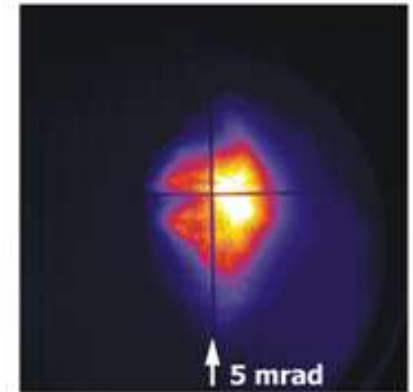
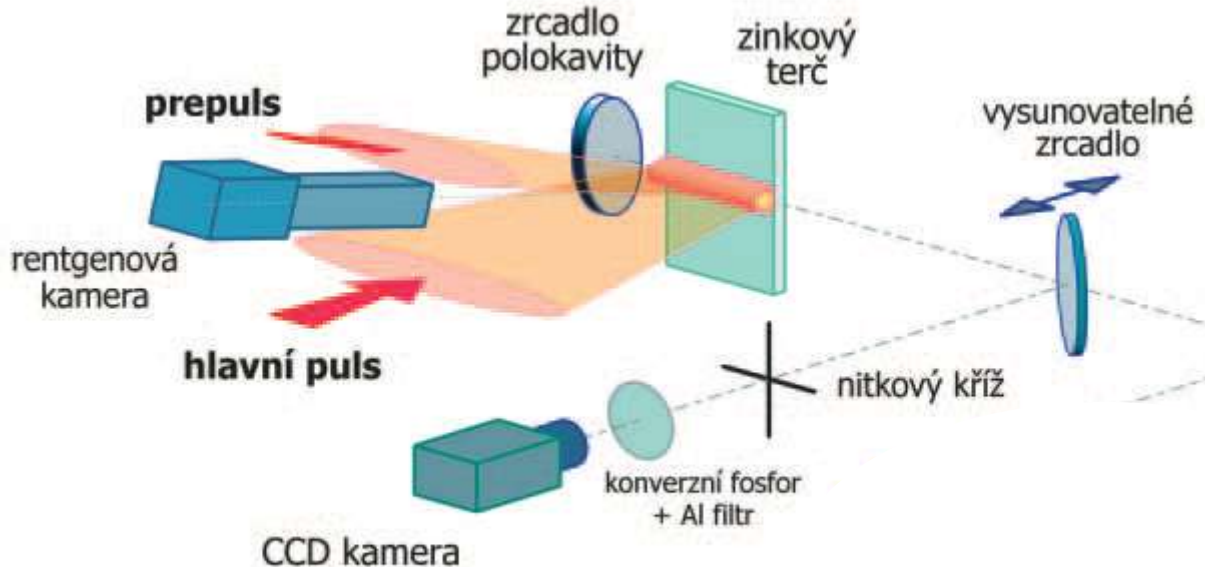
H. Daido, Rep. Prog. Phys. **65** (2002) 1513–1576.

Ne and Ni-like ions are present for wide temperature ranges.

## Ne-like Zn laser at PALS

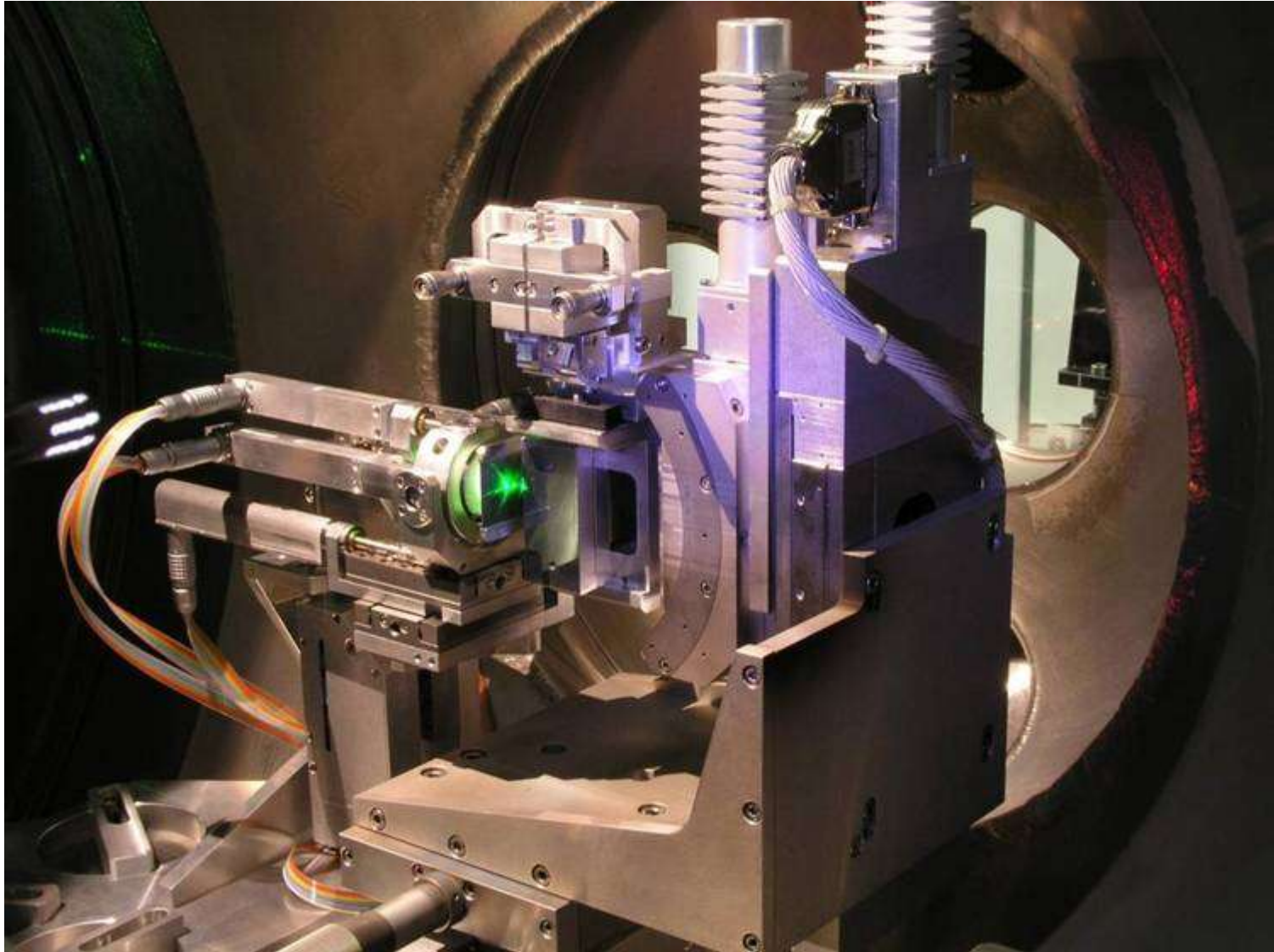
Prepulse (2J) and main pulse (500J) of ASTERIX focused down to a line(150 $\mu$ m) on a 3cm-long Zn target

- Energy 4-10mJ @ 21.2nm ( $\Delta\lambda/\lambda \approx 5 \times 10^{-5}$ )
- Pulse length 150ps
- Beam divergence 3.5 $\times$ 5.5mrad





## Ne-like Zn laser at PALS



# Plasma-based x-ray lasers

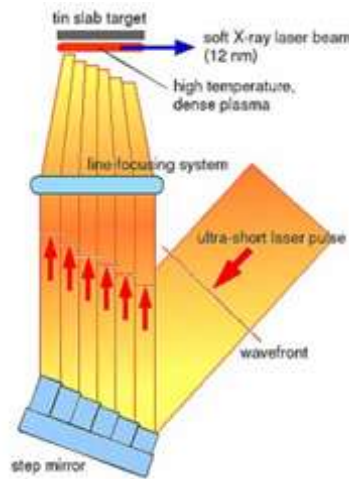
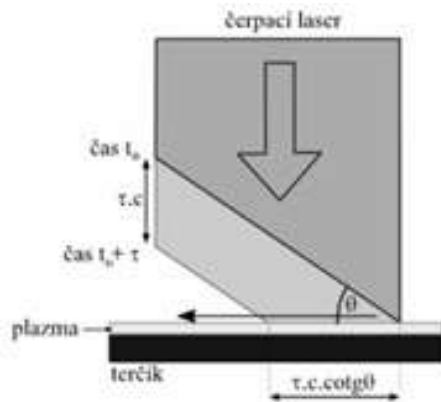
Ni-like ions:

Suitable for shorter  $\lambda$

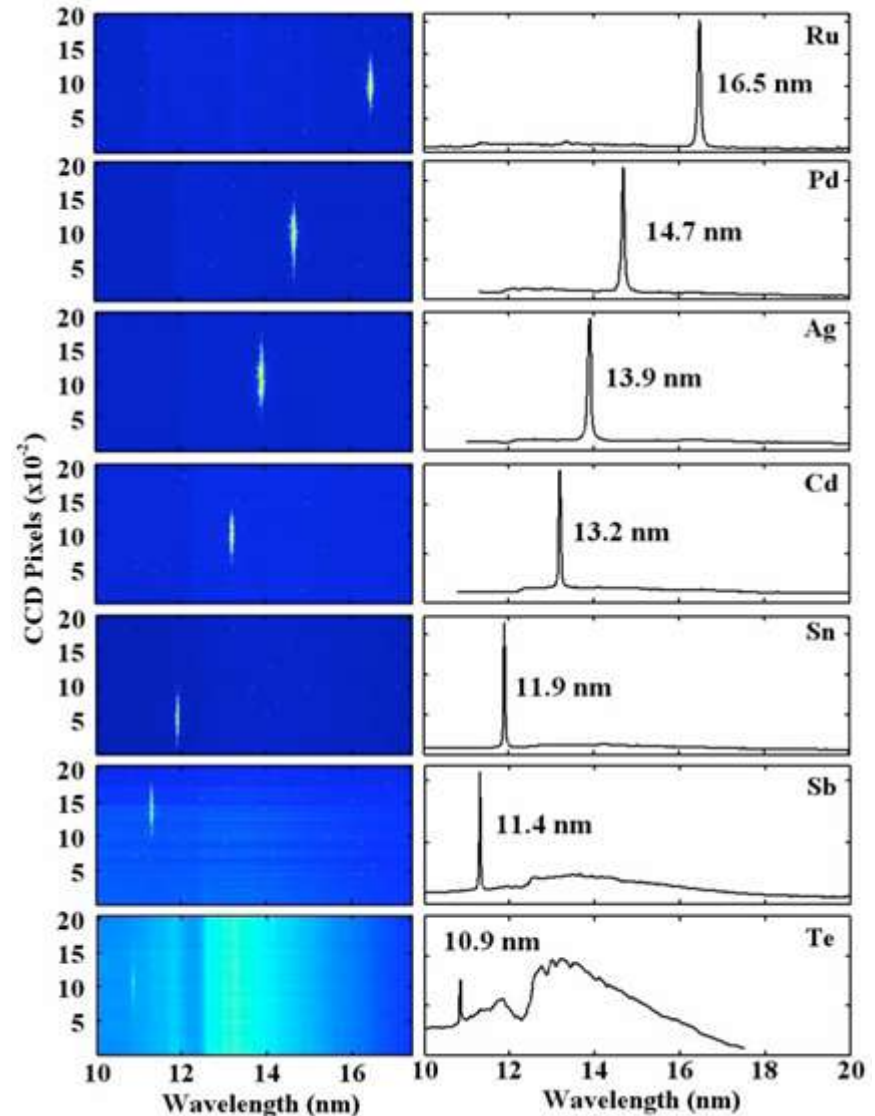
Usually short gain duration– Transient pumping  
Space overlap of pumping with generated radiation

– **Travelling wave**

- Step mirror
- Tilt of the compressor grating



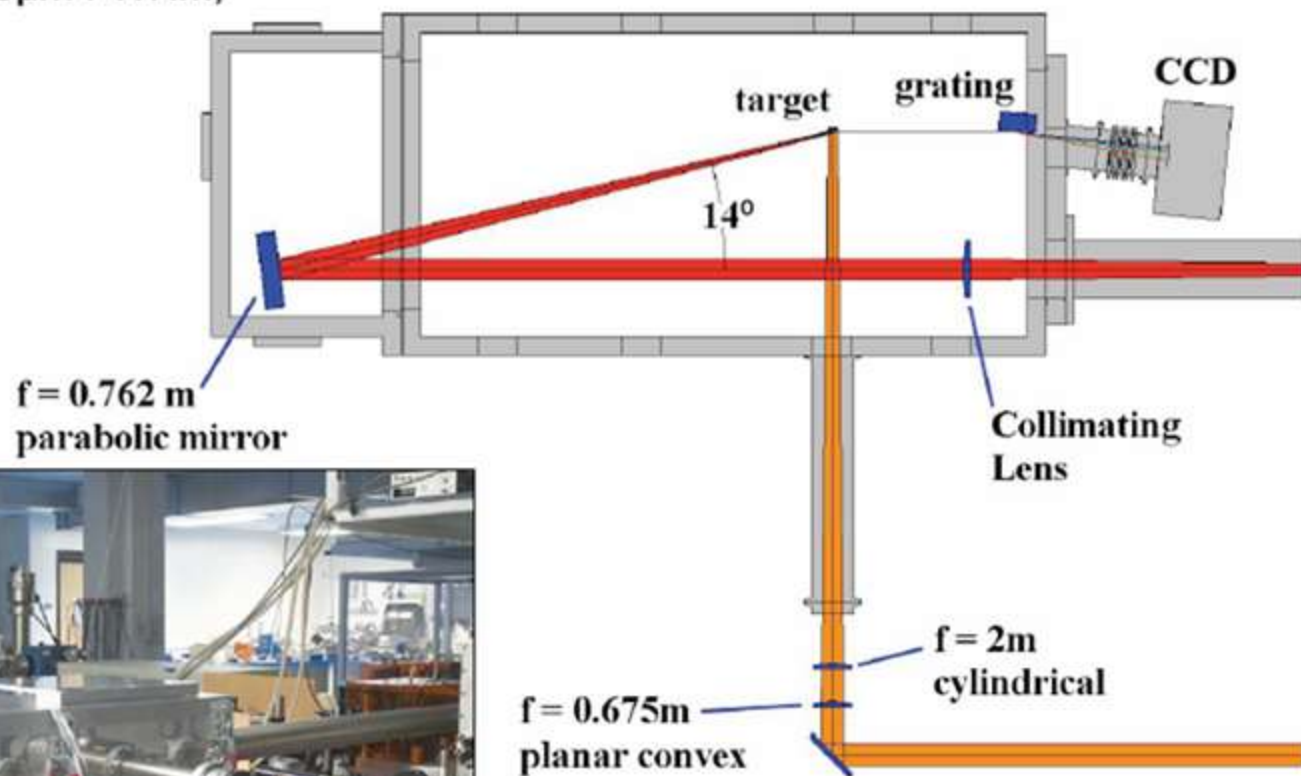
- Longitudinal pumping (gas target)
- GRazing Incidence Pumping



# Configuration for 30 $\mu\text{m}$ wide short pulse line focus at 14 to 26 degrees grazing incidence

## Line Focus

- Pre-pulse: 30 $\mu\text{m}$  FWHM,
- Short-pulse: 30 $\mu\text{m}$  FWHM,



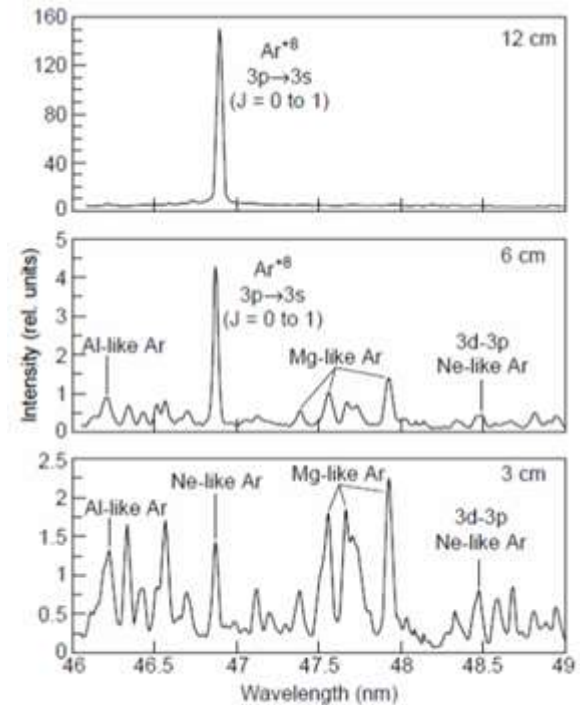
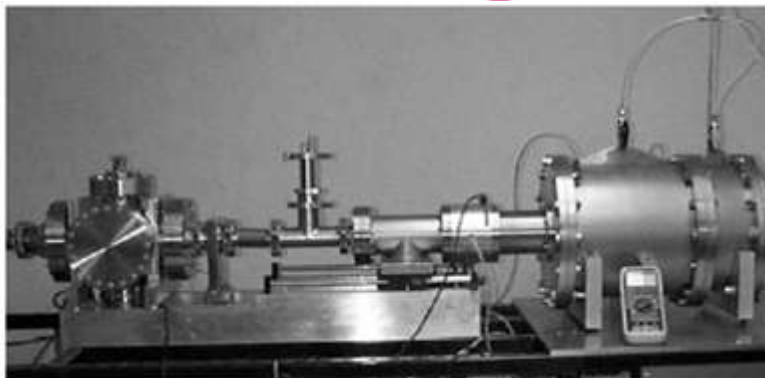
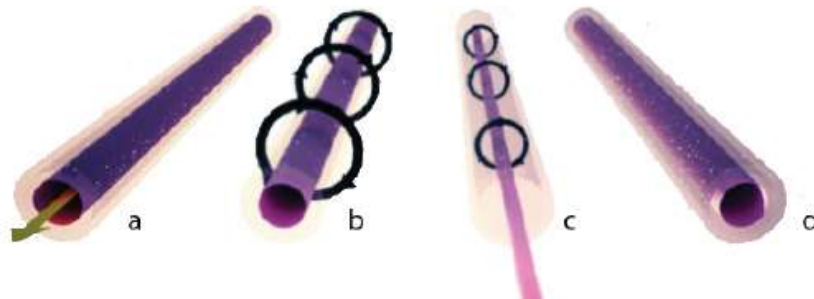
Courtesy of J. Rocca, Colo. State U.

## X-ray laser generated with capillary discharge

Pinch: Strong current compresses (Lorentz force:  $\mathbf{J} \times \mathbf{B}$ ) and heats plasma

- Preionization ( $\sim 10\text{A}$ ,  $\sim 5\mu\text{s}$ )
- Fast strong current pulse ( $I \geq 20\text{kA}$ ,  $\tau \leq 200\text{ns}$ )

Example: Ne-like Ar ( $\text{Ar}^{+8}$ ) na 46.9 nm – suitable for applications

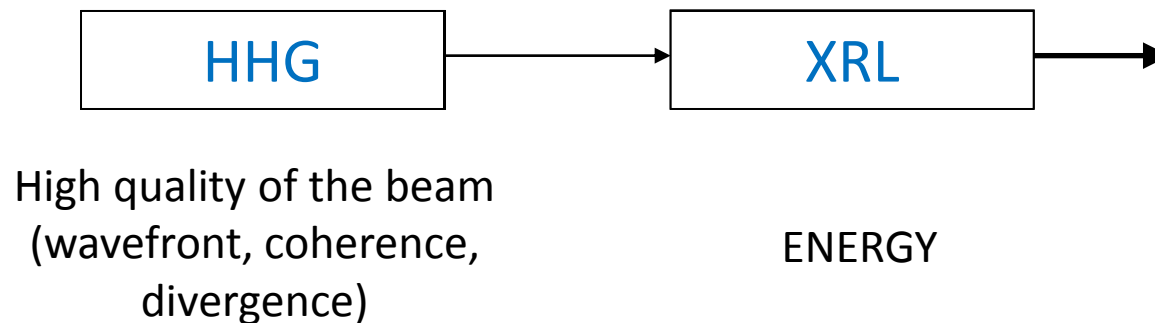


Courtesy of J. Rocca (1995), Colorado State University

# Plasma-based x-ray lasers

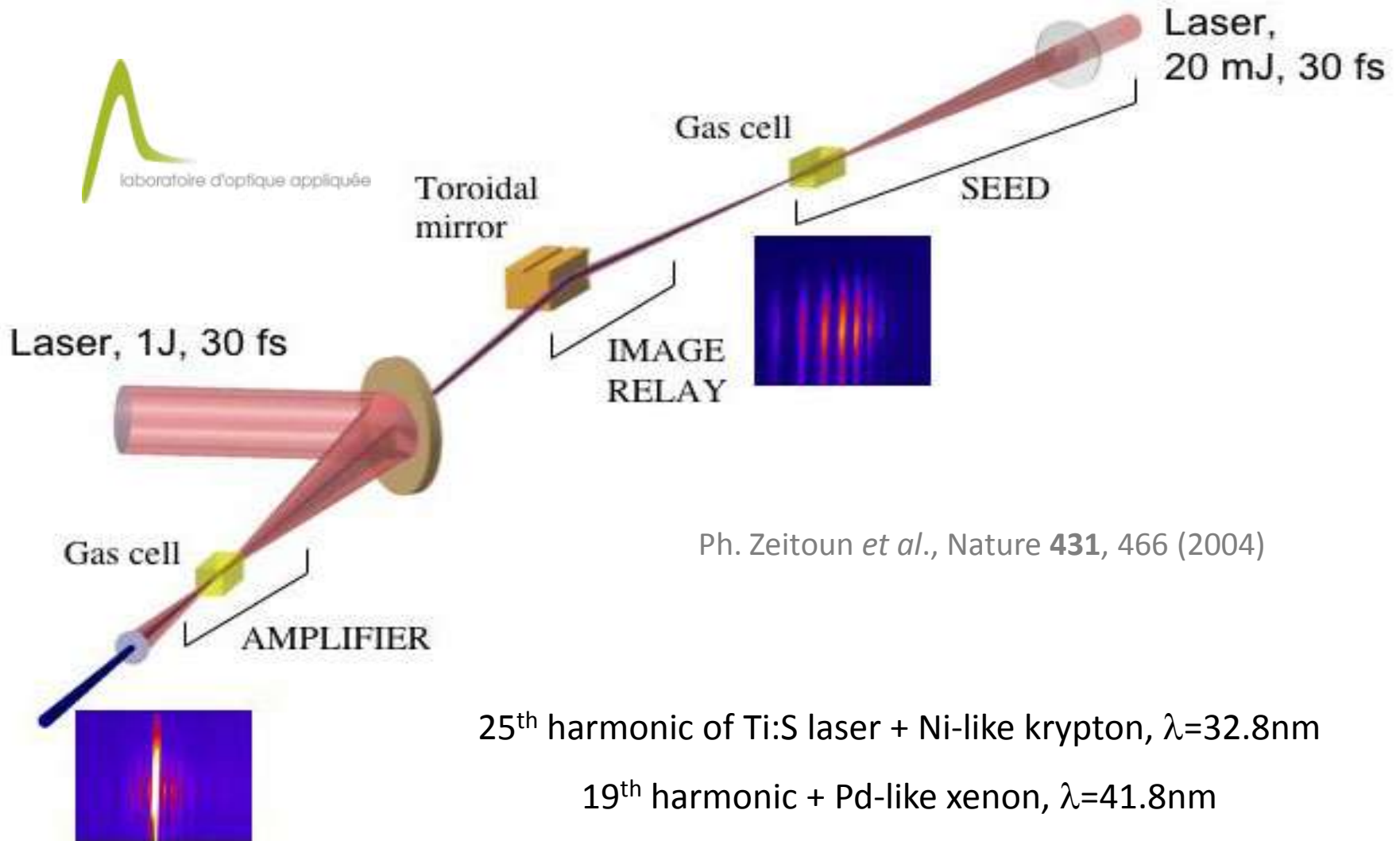
## HHG seed amplified in plasma amplifier (XRL)

Laser chain (Master Oscillator Power Amplifier) in XUV

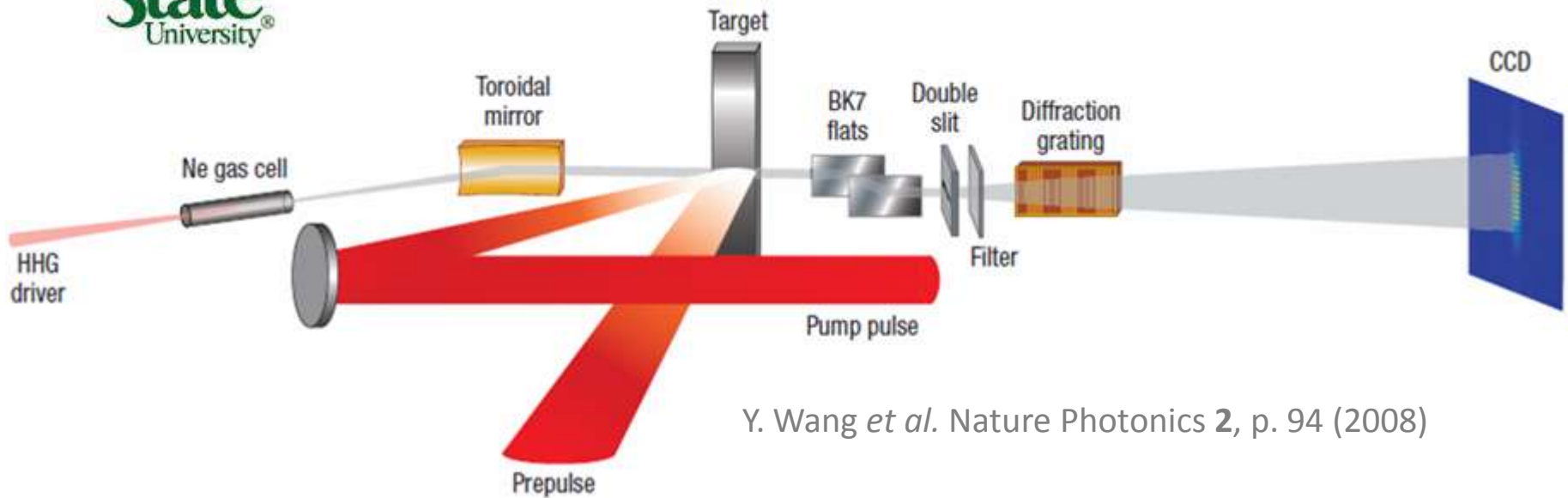


Strong source of fully coherent radiation in XUV/soft x-ray

# Plasma-based x-ray lasers



# Plasma-based x-ray lasers



Y. Wang *et al.* Nature Photonics **2**, p. 94 (2008)

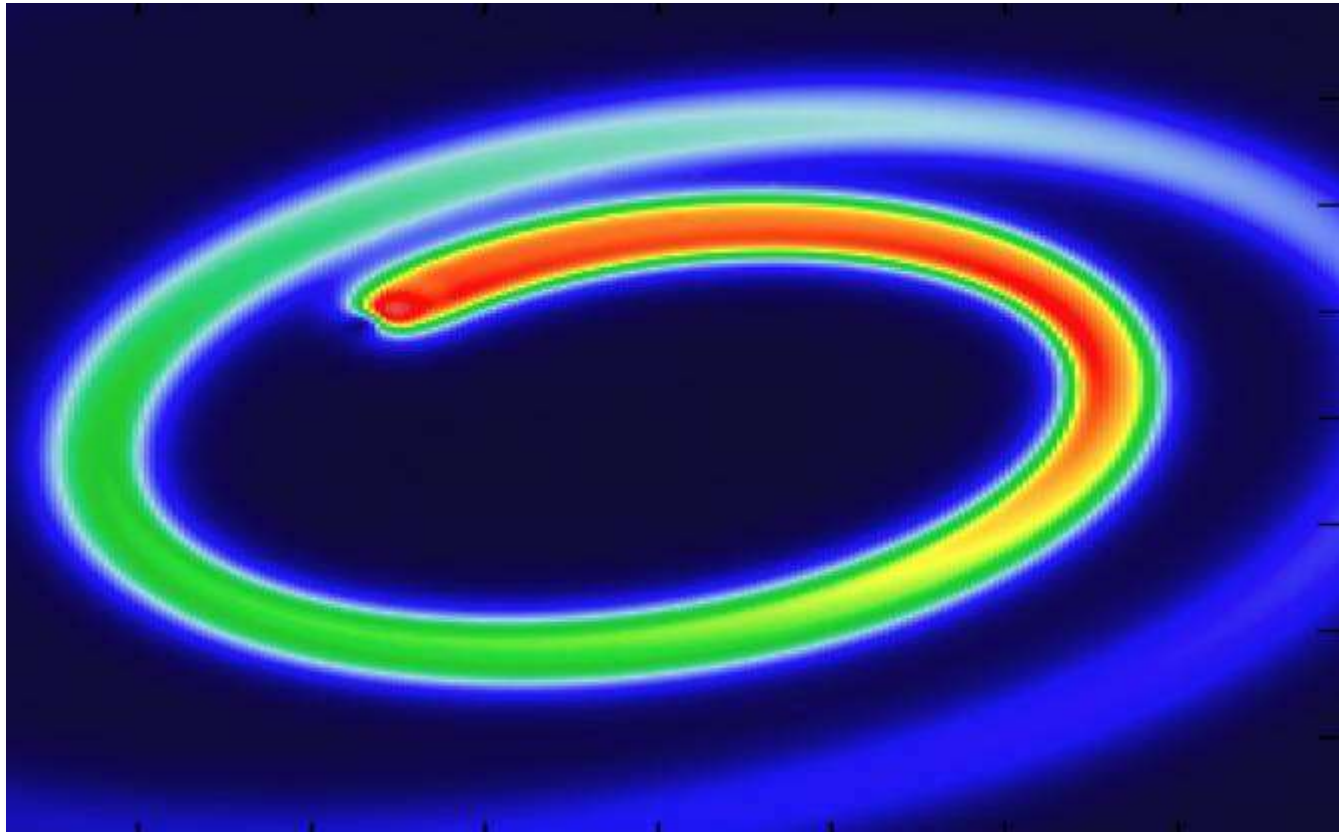
25<sup>th</sup> harmonic of Ti:S laser + Ne-like titan,  $\lambda=32.6\text{nm}$

43<sup>th</sup> harmonic + Ni-like molybden,  $\lambda=18.9\text{nm}$

59<sup>th</sup> harmonic + Ni-like silver,  $\lambda=13.9\text{nm}$

59<sup>th</sup> harmonic + Ni-like cadmium,  $\lambda=13.2\text{nm}$

# Radiation of laser-driven relativistic electron beams

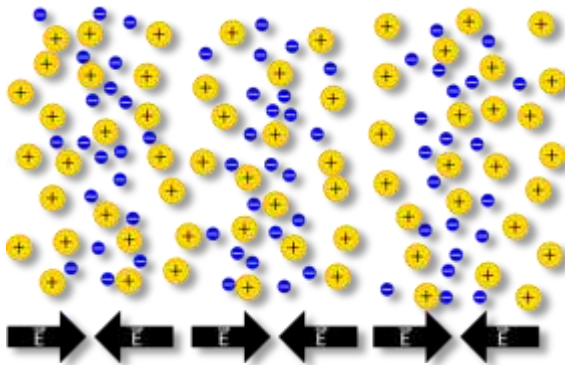


<http://loa.ensta-paristech.fr/>



# Radiation of relativistic e<sup>-</sup> beams

- Electron acceleration in laser plasma
  - Plasma wave behind the laser pulse
  - Huge E-field >100 GV/m possible (conventional RF accelerators <0.1GV/m)

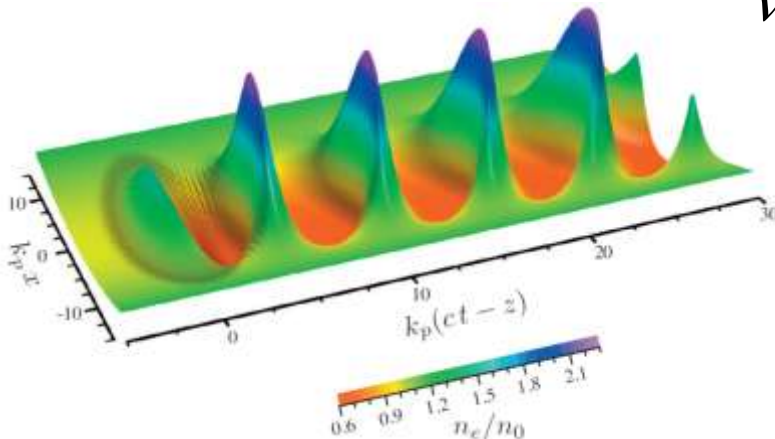


plasma frequency:

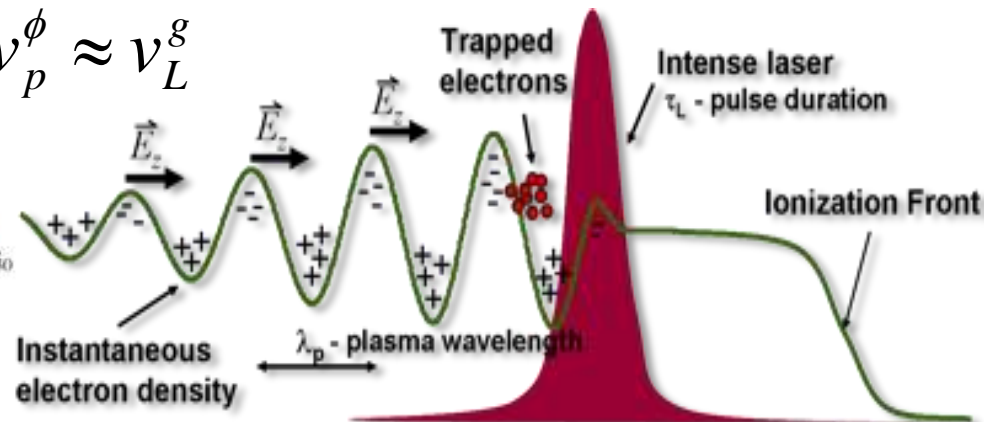
$$\omega_p^2 = \frac{n_e e^2}{\epsilon_0 m_e}$$

ponderomotive force:

$$F_p = -\frac{e^2}{2\epsilon_0 c m_e \omega^2} \nabla I$$



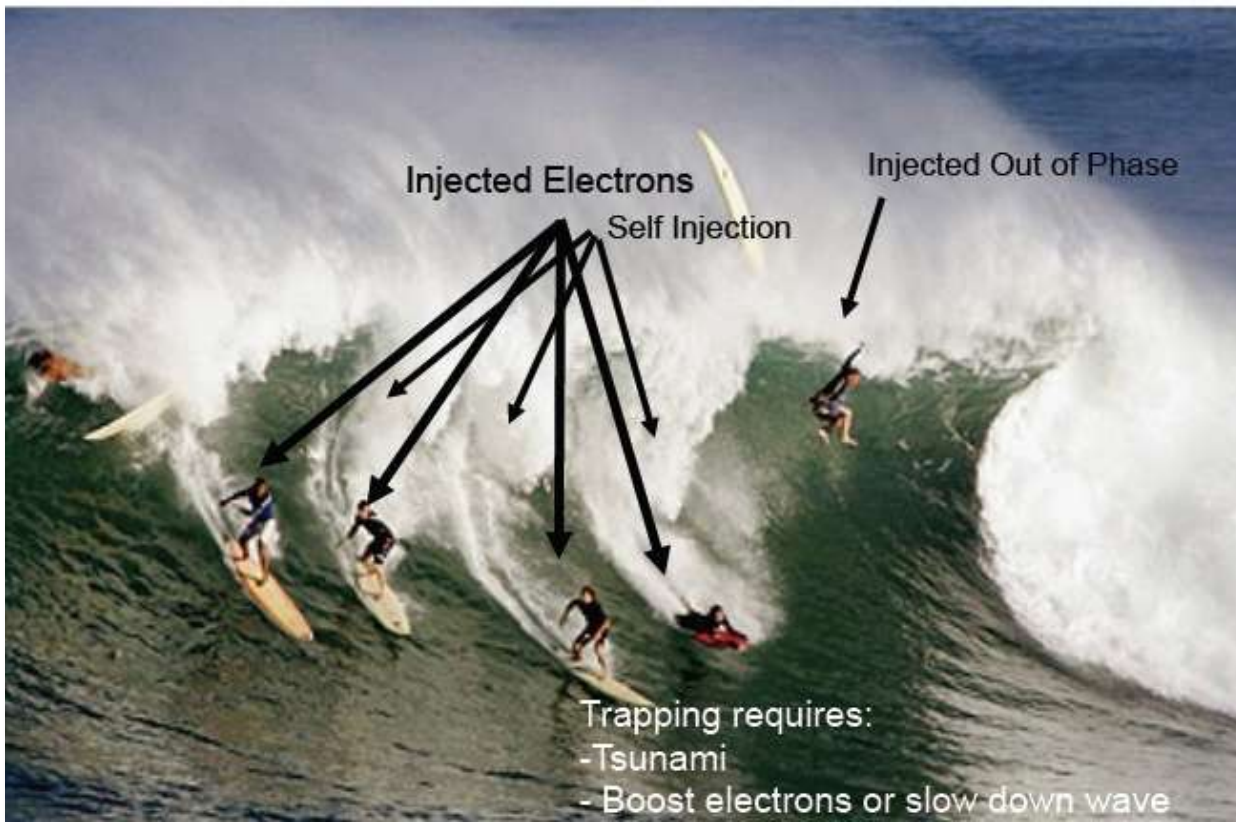
$$v_p^\phi \approx v_L^g$$



[www.engin.umich.edu/research/cuos](http://www.engin.umich.edu/research/cuos)

# Radiation of relativistic $e^-$ beams

- Electron acceleration in laser plasma
  - Plasma wave behind the laser pulse
  - Huge E-field  $> 100$  GV/m possible (conventional RF accelerators  $< 0.1$  GV/m)



# Radiation of relativistic e<sup>-</sup> beams

- Electron acceleration in laser plasma

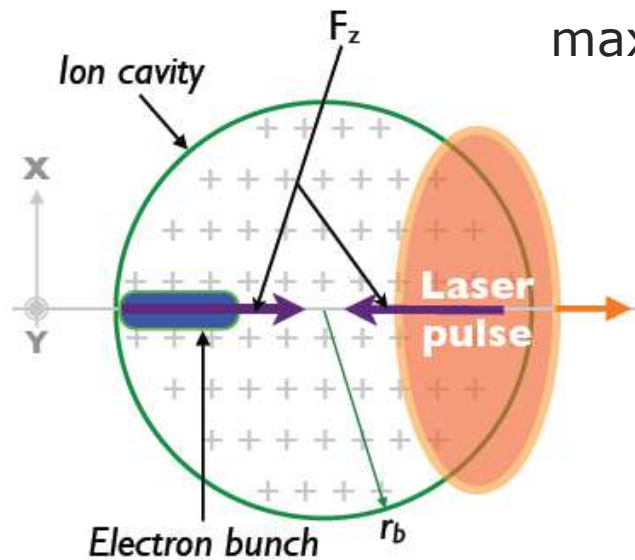
- If the parameters are set right: **bubble regime**

- Focus size and intensity vs. plasma density

- Laser pulse duration vs. plasma density

$$\tau \approx \frac{\pi}{\omega_p} \quad \frac{2\sqrt{a_0}}{w_0} \approx \frac{\omega_p}{c}$$

$a_0 > 2 \Rightarrow$  ion cavity (no electrons) behind the laser pulse  
 wavebreaking – acceleration of e<sup>-</sup>



maximum field:  $E_m = \frac{m_e c}{e} \omega_p \sqrt{a_0}$

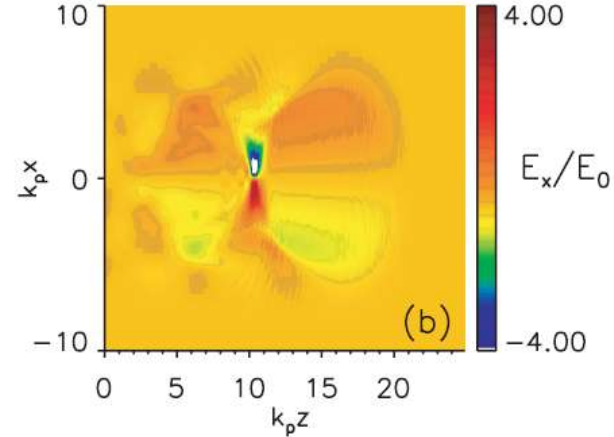
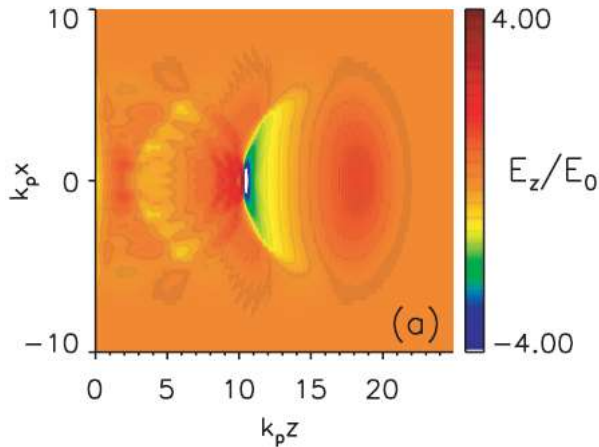
$a_0 \approx 4, \tau \approx 30 \text{ fs} \Rightarrow n_e = 10^{19} \text{ cm}^{-3}$

$E_m \approx 600 \text{ GV/m}$



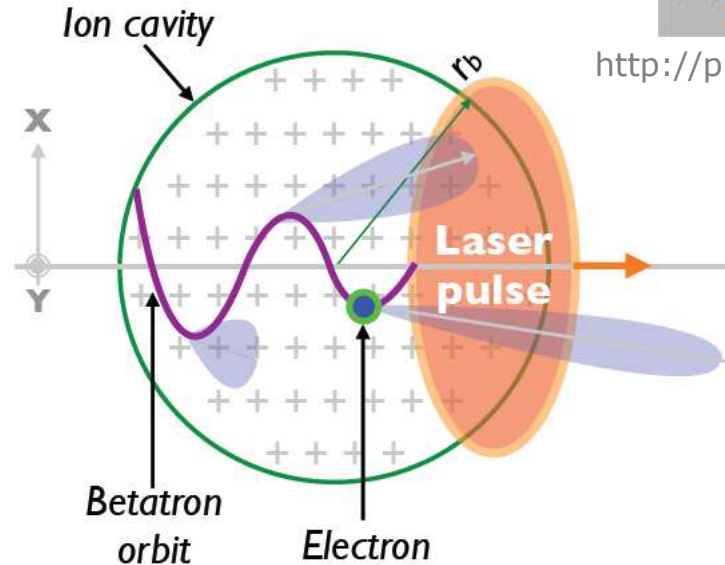
# Radiation of relativistic $e^-$ beams

- Besides the longitudinal there is also transverse field



⇒ Oscillations of electron beam ⇒ RADIATION

so called **plasma betatron**

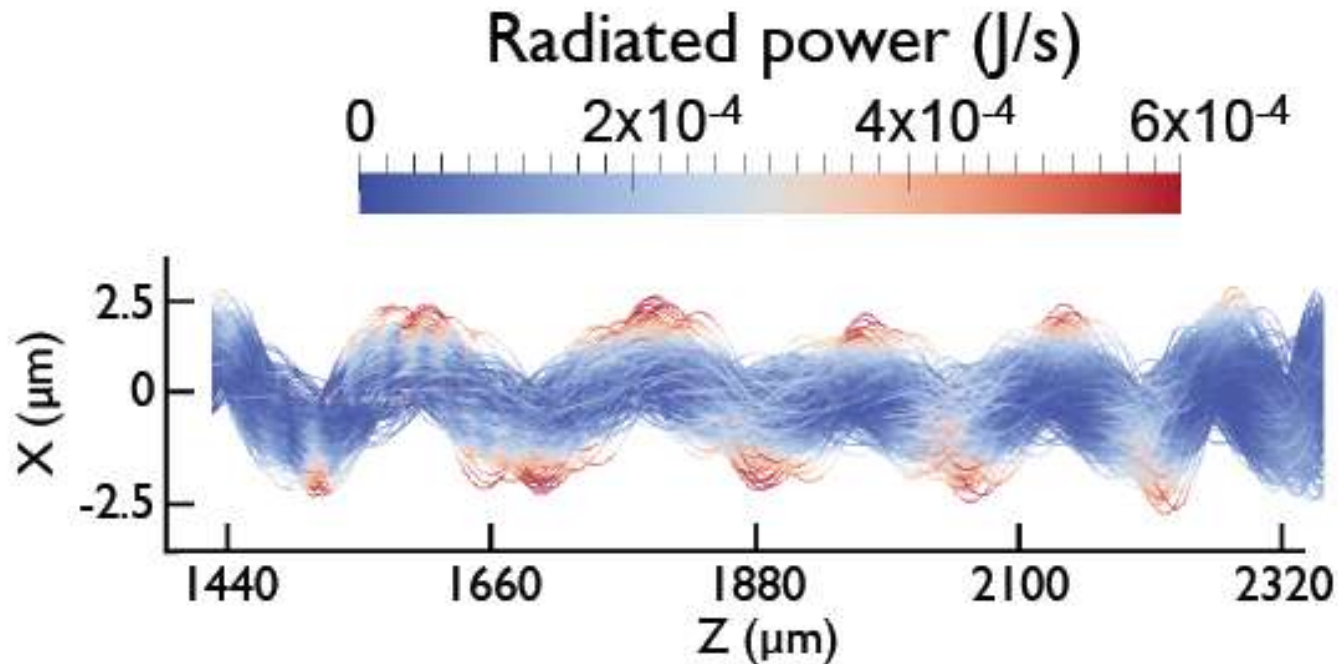


<http://picongpu.fzd.de>

# Radiation of relativistic e<sup>-</sup> beams

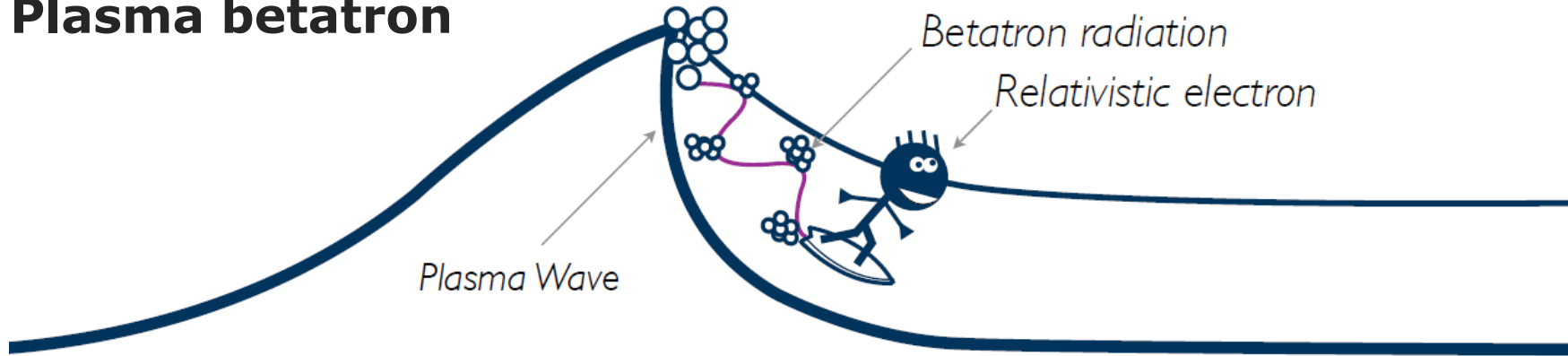
## Plasma betatron

$$\frac{d^2I}{d\omega d\Omega} = \frac{e^2}{4\pi^2 c} \left| \int_{-\infty}^{+\infty} e^{i\omega[t - \vec{n} \cdot \vec{r}(t)/c]} \frac{\vec{n} \times [(\vec{n} - \vec{\beta}) \times \dot{\vec{\beta}}]}{(1 - \vec{\beta} \cdot \vec{n})^2} dt \right|^2$$



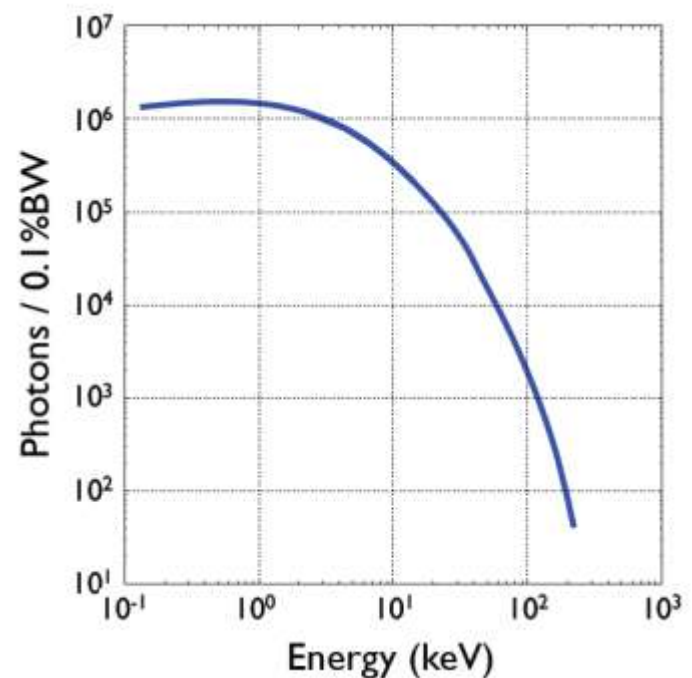
# Radiation of relativistic e<sup>-</sup> beams

- **Plasma betatron**



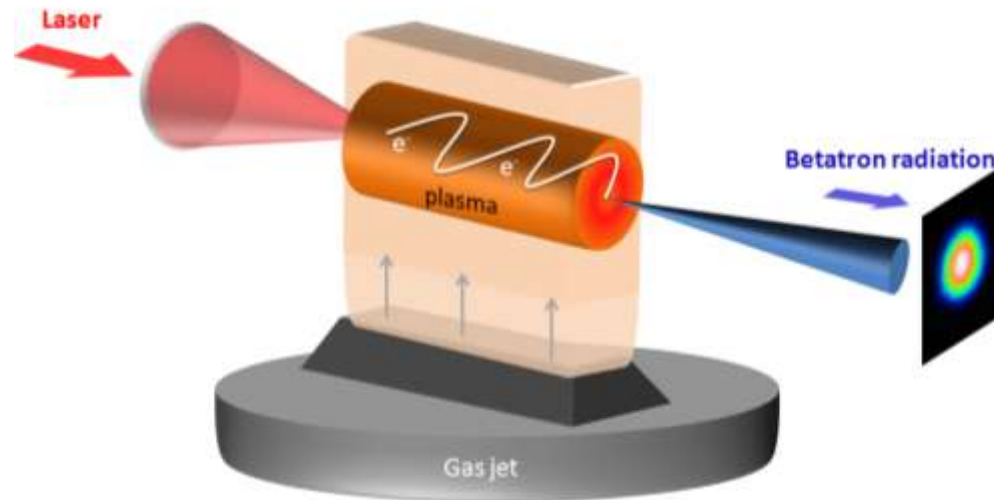
Typical spectrum:

- High energy radiation
- Polychromatic
- Ultra-short pulses (<50fs)
- small source size (<10 $\mu$ m)

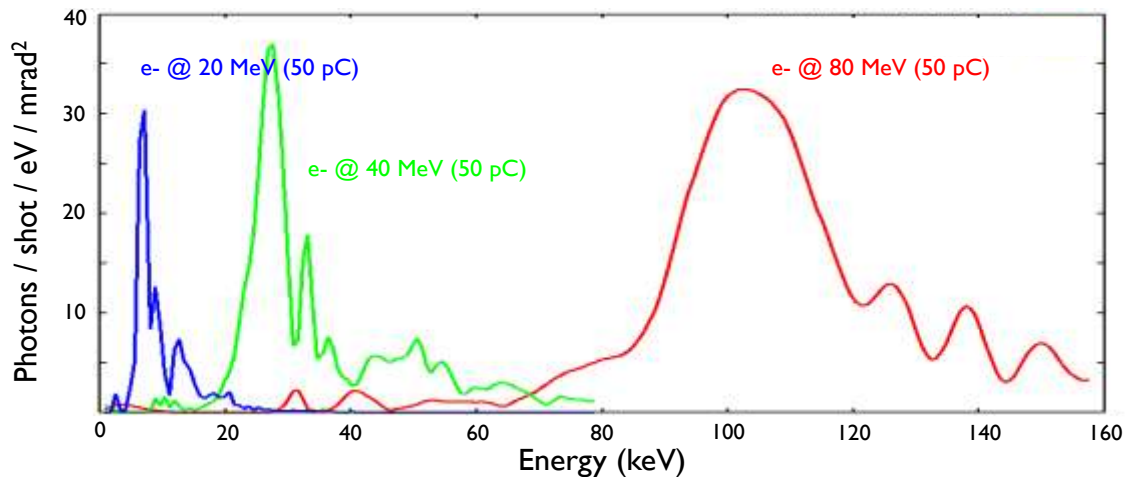


# Radiation of relativistic $e^-$ beams

- Plasma betatron



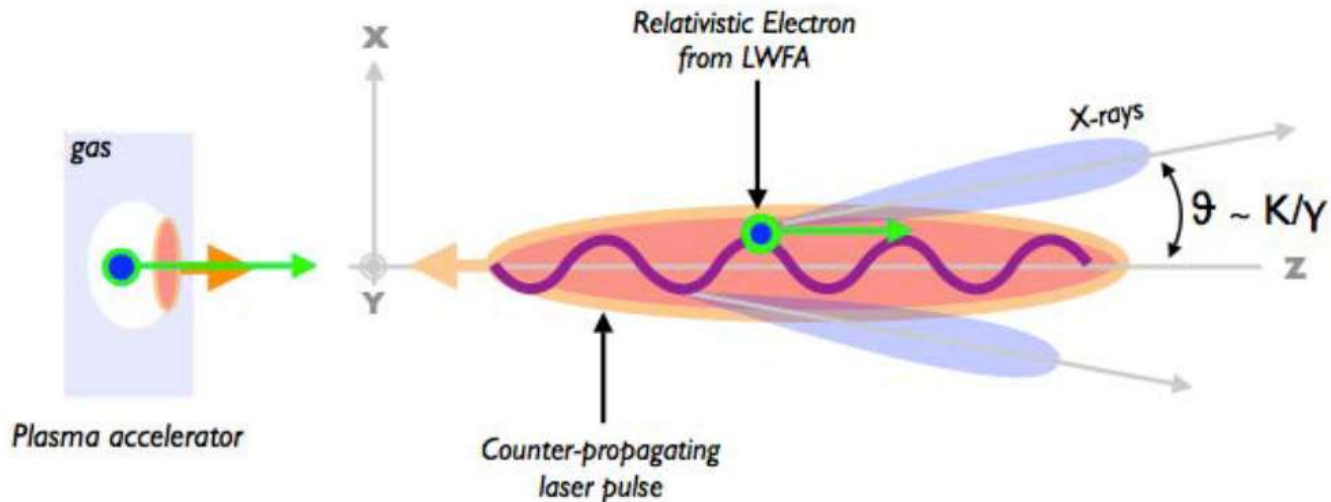
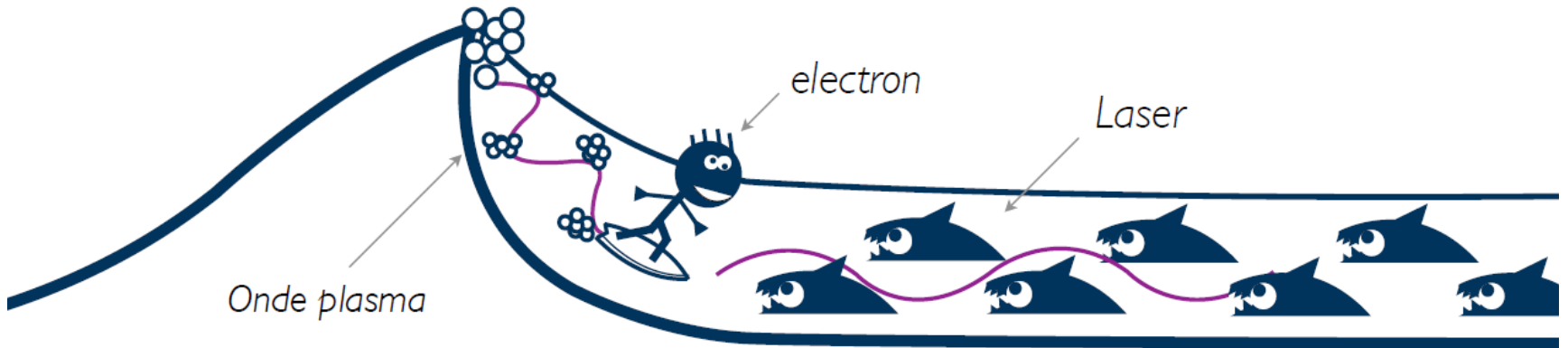
In the case of monoenergetic electron beams:



# Radiation of relativistic e<sup>-</sup> beams

- **Thomson back-scattering** (inverse Compton scattering)

Interaction e<sup>-</sup> with an intense laser pulse

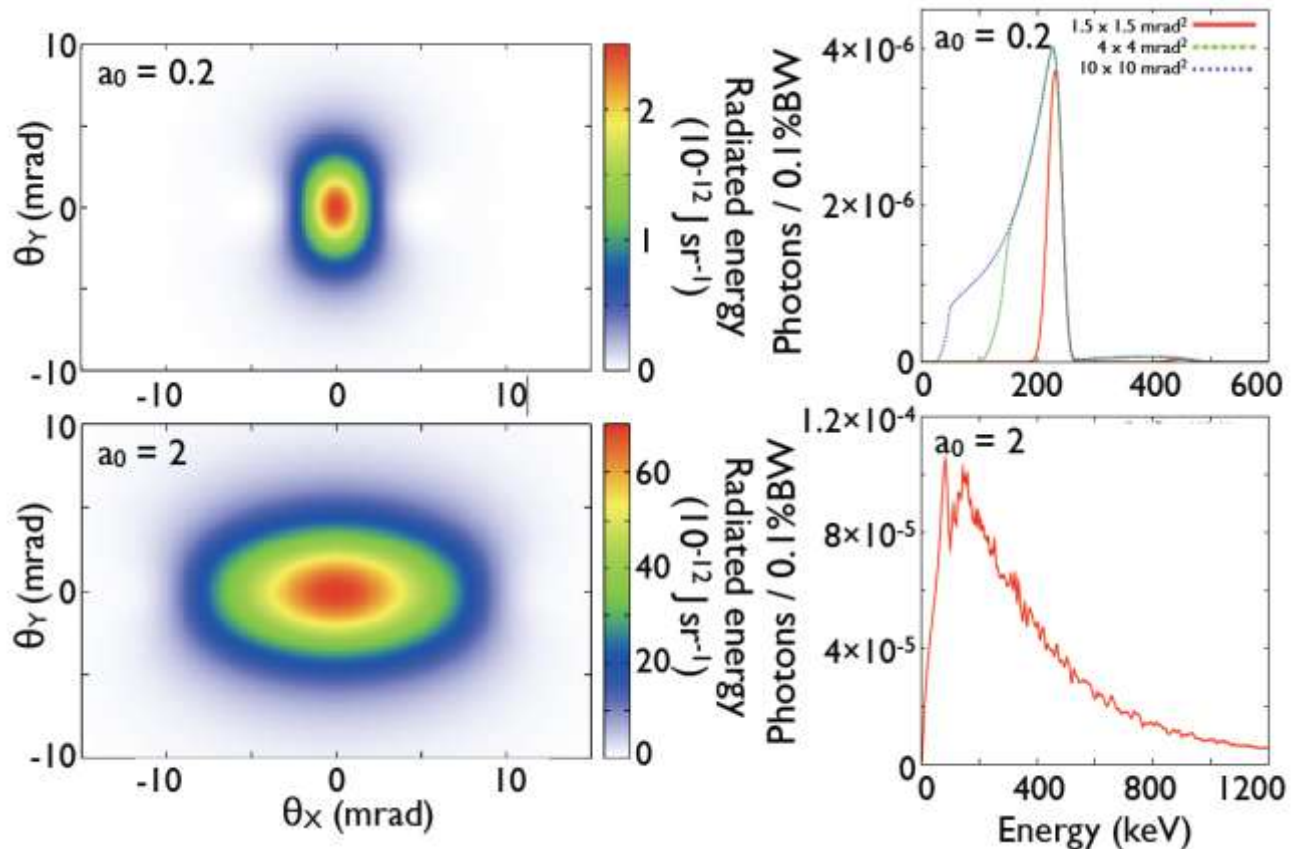




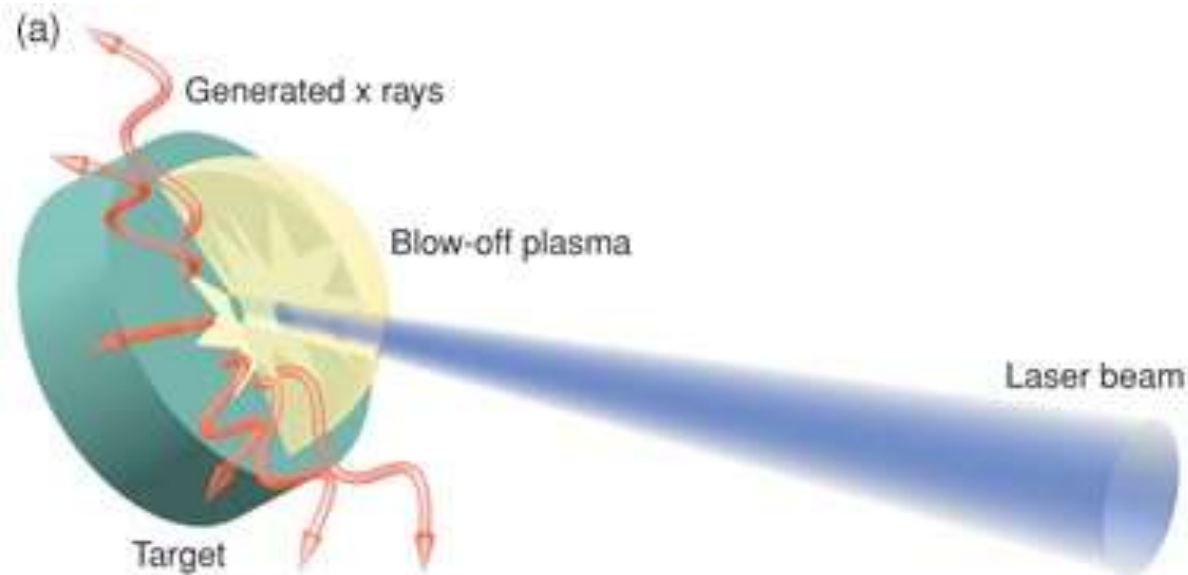
# Radiation of relativistic e<sup>-</sup> beams

- Thomson back-scattering

- very hard radiation (up to MeV)  $\omega_X = 4\gamma^2\omega_L$

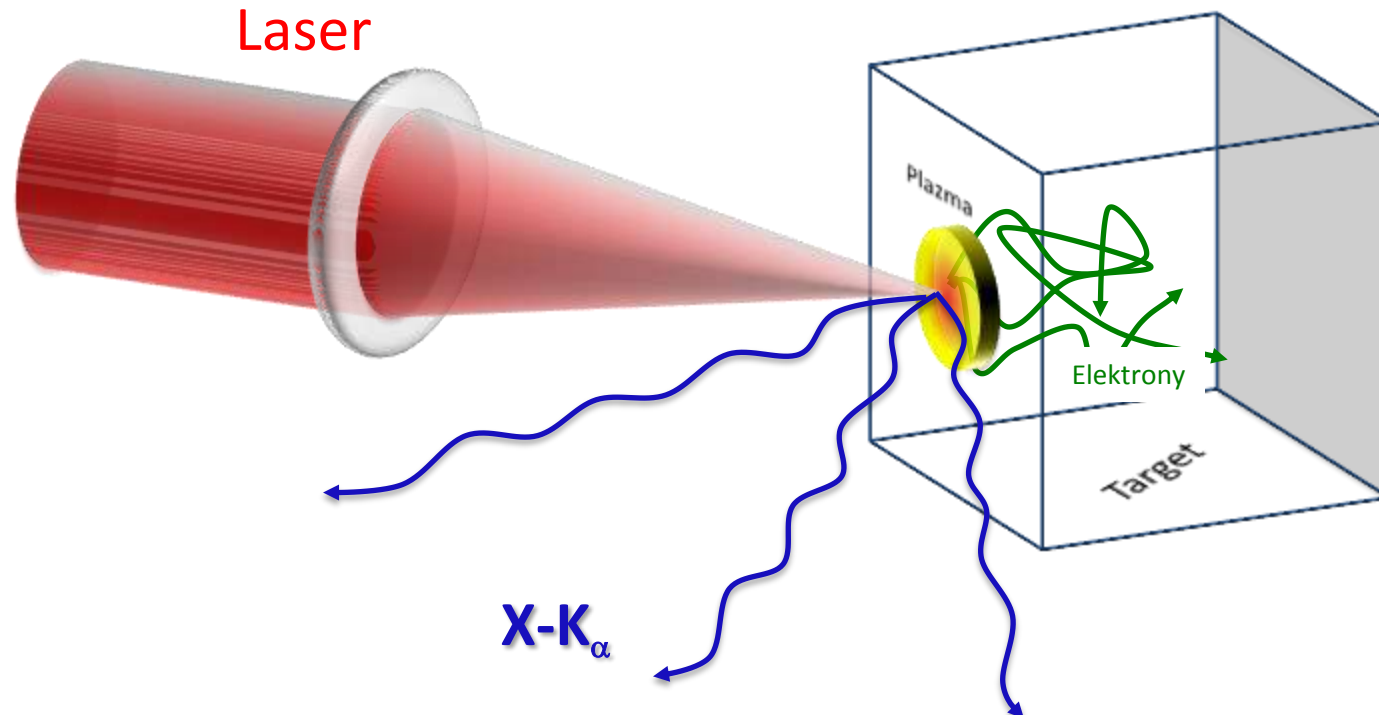


# X-ray plasma source ( $K\alpha$ )



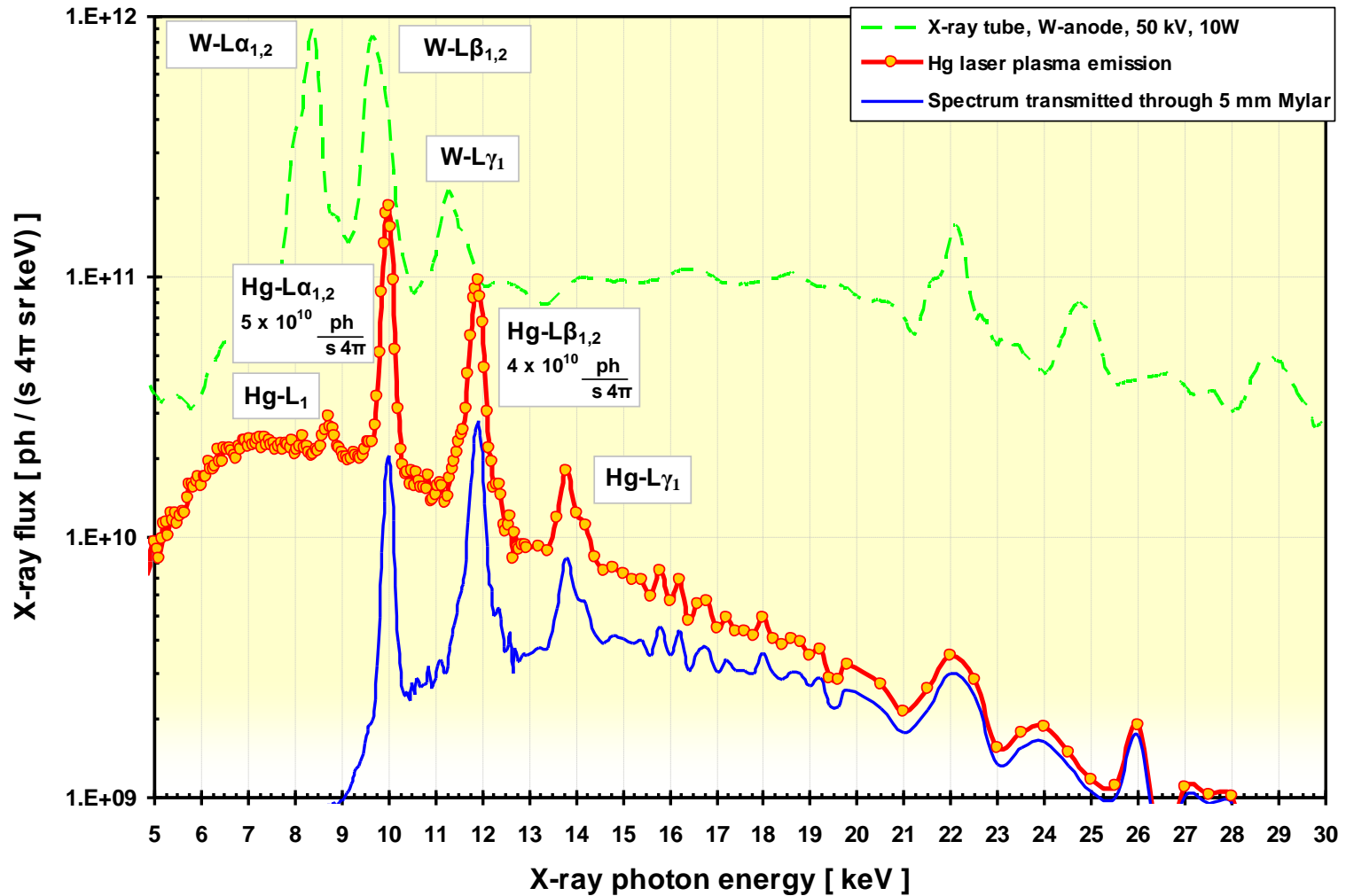
# X-ray plasma source

- Creation of “hot” electrons by interaction of intense laser pulse with matter ( $I > 10^{16} \text{ Wcm}^{-2}$ )  $T_h \propto I\lambda^2$
- Energetic electrons are decelerated in the target
  - generation of bremsstrahlung and characteristic radiation



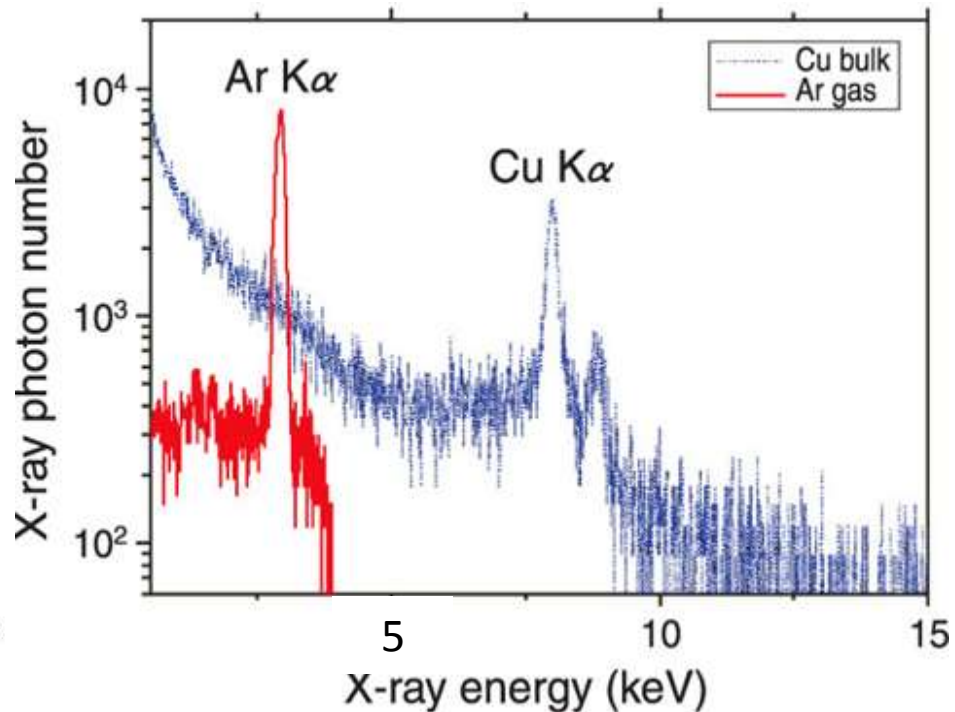
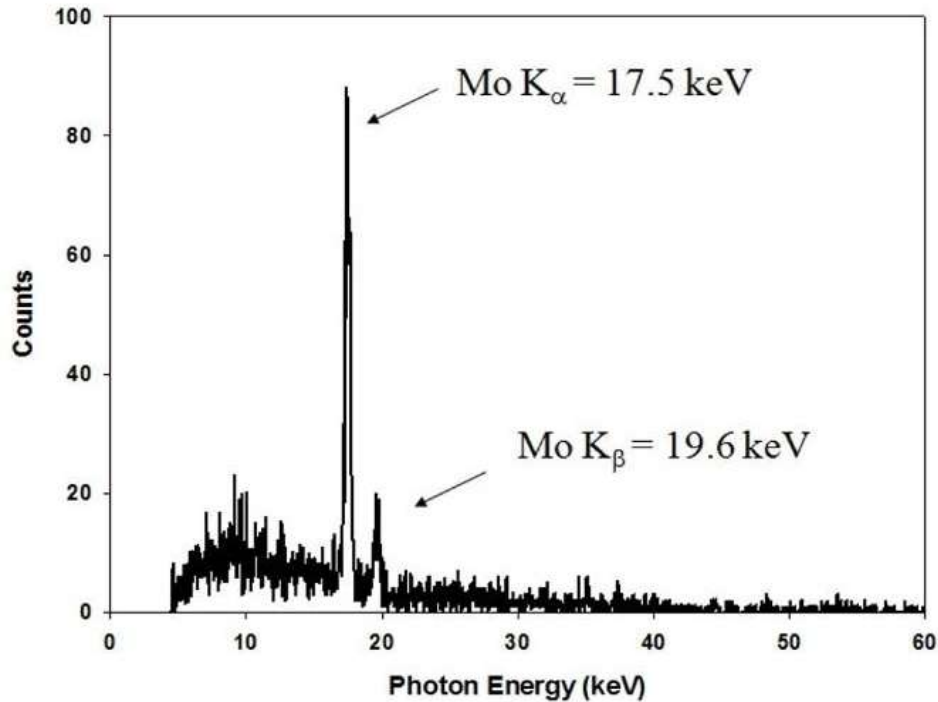
# X-ray plasma source

- Spectrum similar with an x-ray tube



# X-ray plasma source

- Tuning parameters  $\Rightarrow$  strong  $K\text{-}\alpha$  line emission



- Incoherent, polychromatic
- Isotropic emission ( $4\pi$ )
- Short pulse duration ( $\sim 100$  fs)

# Future research facility ELI Beamlines

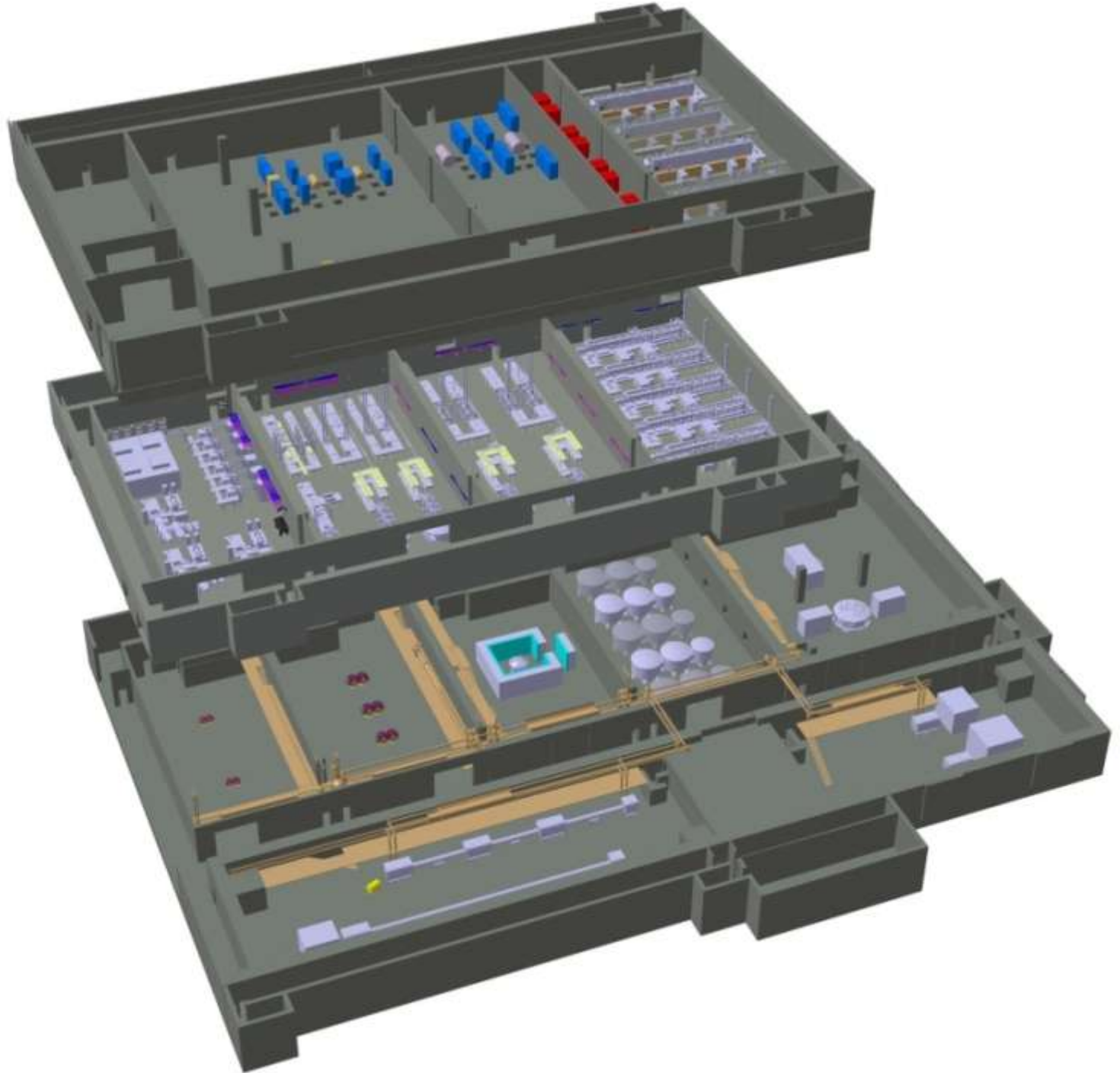


# Future research facility ELI Beamlines

## Dolní Břežany near Praha



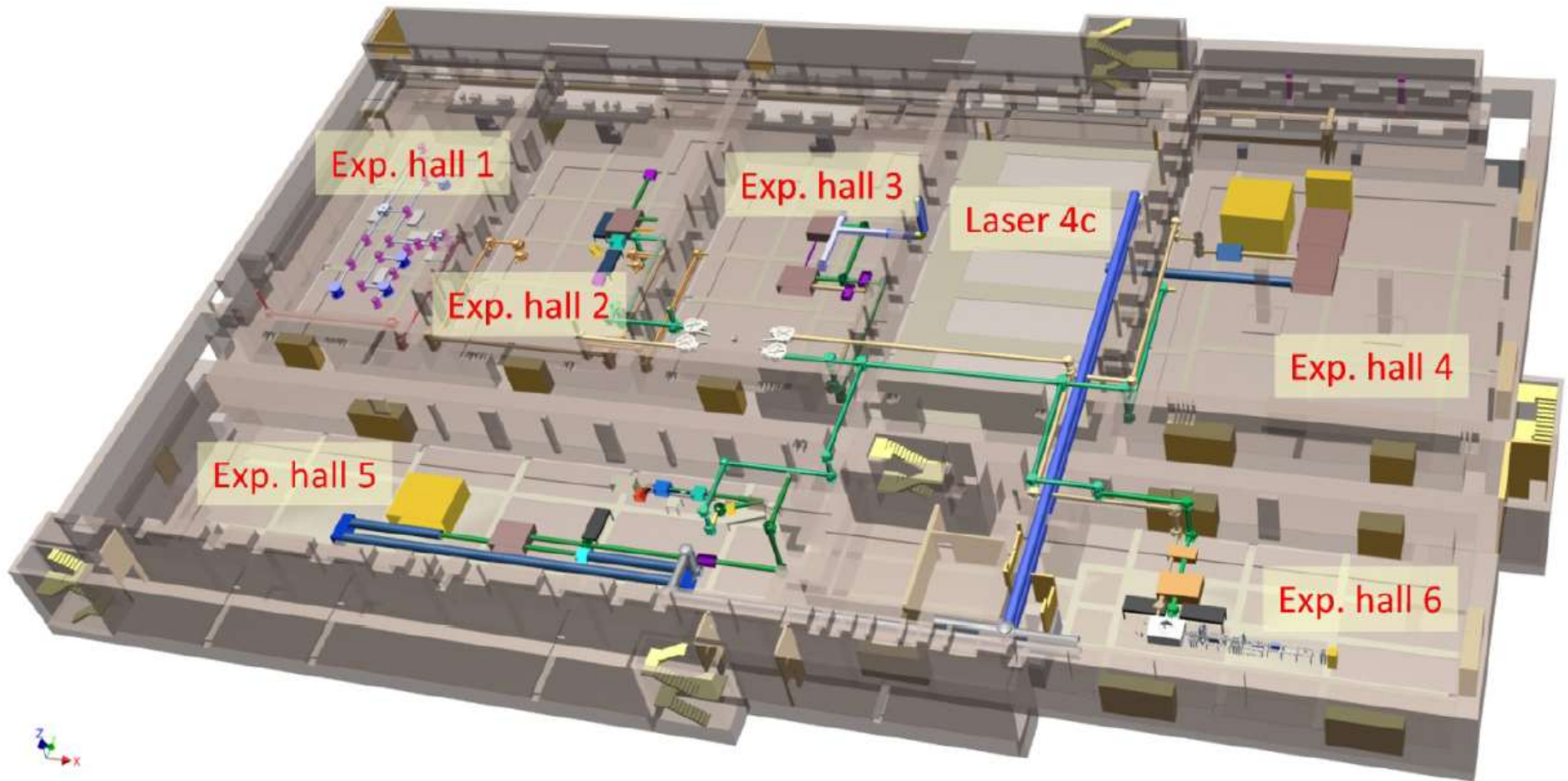
Dolní Břežany





# Future research facility ELI Beamlines

## Experimental halls





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# THANK YOU FOR YOUR ATTENTION

Any cooperation is highly welcome

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